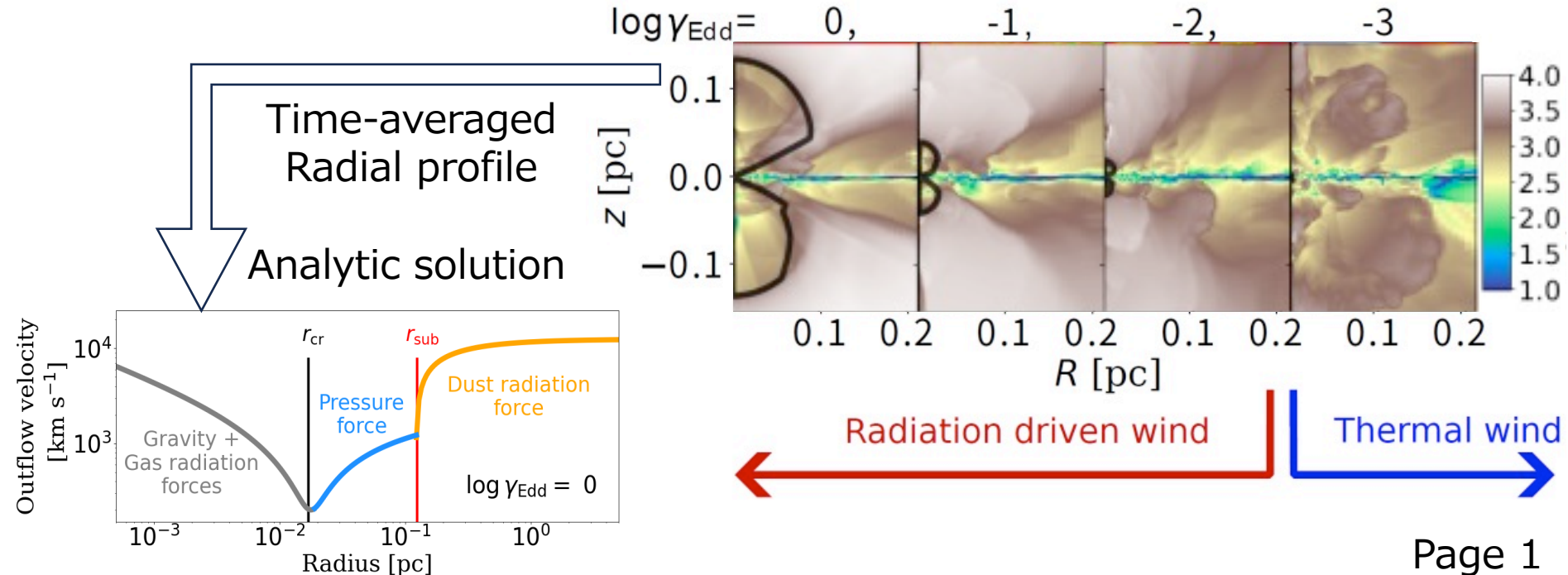


# Dust-free and dusty outflows in sub-parsec region of AGN

Yuki Kudoh (Tohoku Univ.)

Keiichi Wada (Kagoshima Univ.),

Kawakatu Nozomu (Kure Collage), Mariko Nomura (Hirosaki Univ.)



# AGN unified model : Gas structure

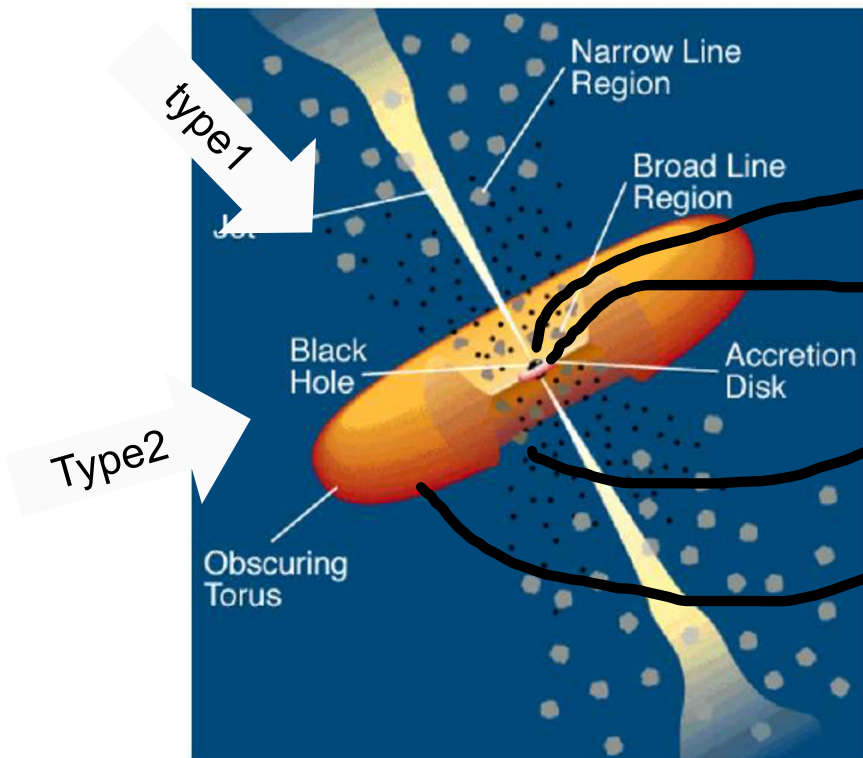
Antonucci 1993, Urry & Padvani 1998

The unified model of AGNs is composed of the structures:

SMBH, accretion disk, broad-line region (BLR), and dusty torus.

This model explains observations such as:

- Broad emission lines, visible (Type 1) or invisible (Type 2),
- Continuum from IR to X-rays.



Spatial scale @  $10^7 M_{\odot}$

SMBH

$\sim 1 R_g \sim 10^{-6} \text{ pc}$

Accretion disk

$\sim 100 R_s \sim 10^{-4} \text{ pc}$

**BLR**

$\sim 10^3 R_s \sim 10^{-3} \text{ pc}$

**Torus**

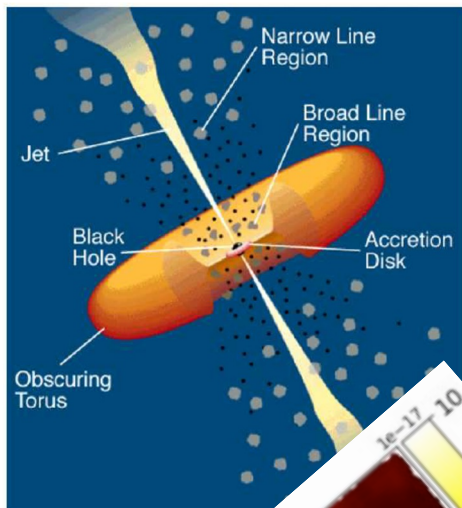
$\sim 10^6 R_s \sim 1 \text{ pc}$

# Ionized (multiphase) dusty outflow

## AGN gas unification

Antonucci 1993

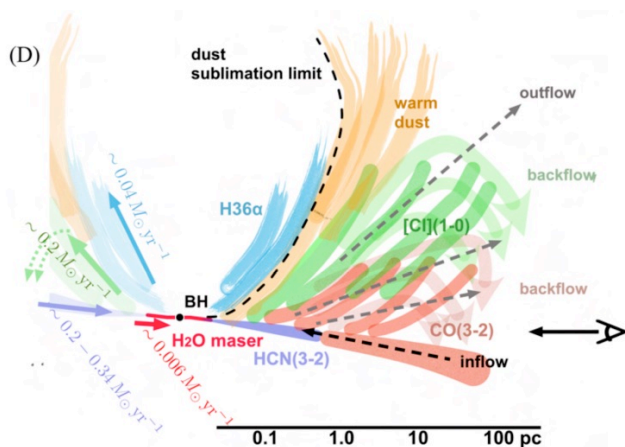
Urry & Padvani 1998



## Multiphase outflow

Circinus galaxy

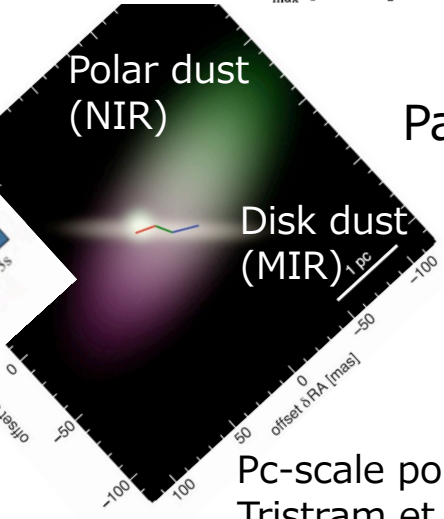
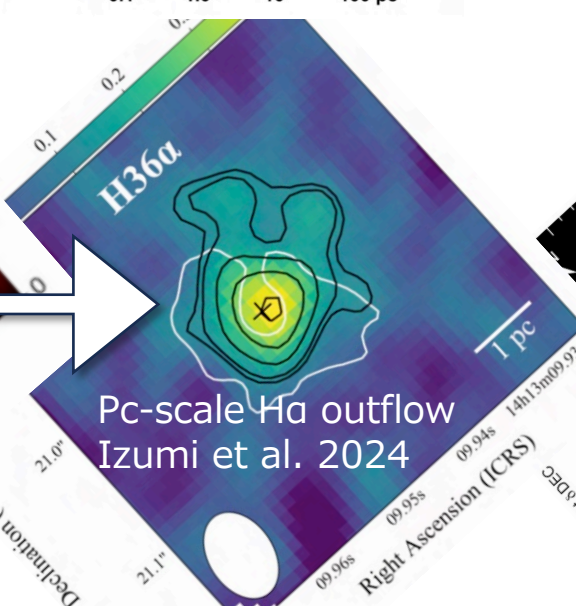
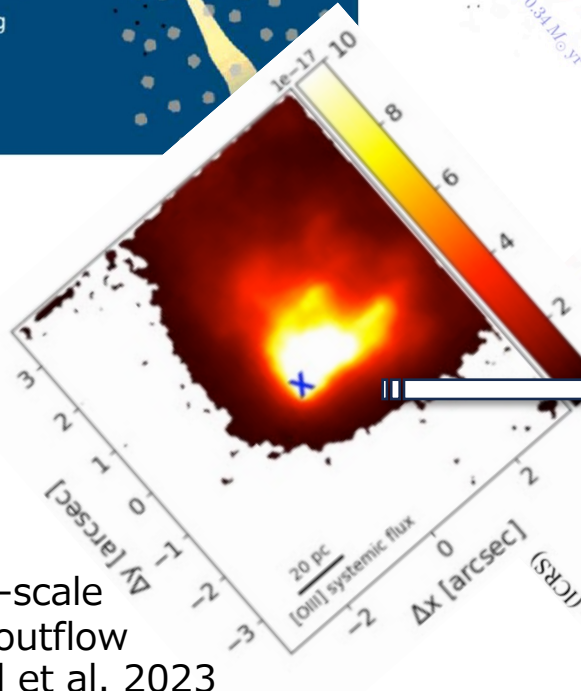
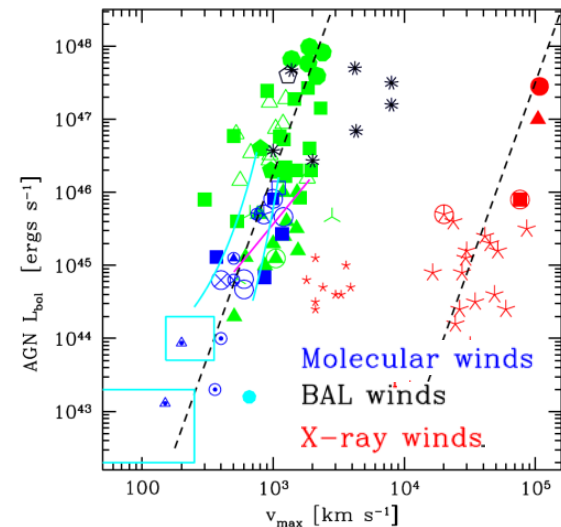
Izumi et al. 2023



## Correlation: $v_{\text{out}}$ & $L_{\text{bol}}$

Fiore et al. 2016

$10^2 - 10^5 \text{ km s}^{-1}$



# How does gas move near the dust sublimation radius?

- Dust temperature  $T_{\text{dust}}$  can be estimated from local thermal equilibrium (LTE) with the AGN irradiation and re-emission.
- If  $T_{\text{dust}} > T_{\text{sub}} \approx \mathbf{1500\text{ K}}$ , dust is destroyed.
- The size of the dust-destroyed region is the **sublimation radius**  $r_{\text{sub}}$ .
- $r_{\text{sub}}$  is given by

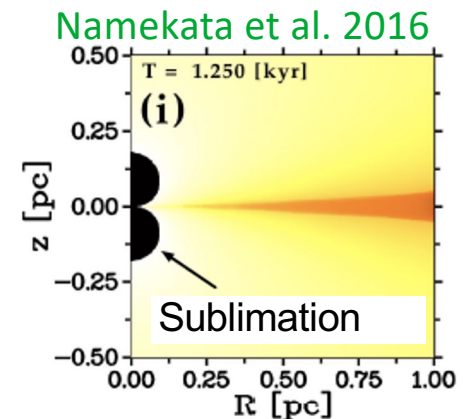
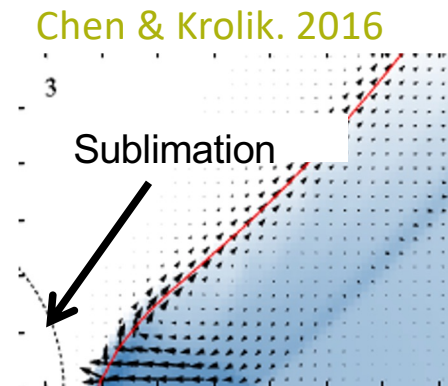
$$r_{\text{sub}} \approx 0.05 \left( \frac{L_{\text{AGN}}}{10^{44} \text{ erg/s}} \right)^{1/2} \left( \frac{T_{\text{sub}}}{1500 \text{ K}} \right)^{-2} \text{ pc}$$

→ sub-parsec scale.

However, previous studies mainly simulated the region outside  $r_{\text{sub}}$ .

## Aim:

- Perform simulations resolving both dust-surviving and dust-destroyed regions.
- Investigate dynamical structure of AGN outflows.



# Simulation model

## Physics (Kudoh et al. 2023)

- Dust-radiation-hydrodynamic equation
- SMBH gravity
- Dust
  - $M_{\text{BH}} = 10^7 M_{\odot}$
  - Dust-gas mass ratio = 0.01
  - Radiation force modeled by opacity
  - Dust destruction :  
sublimation, thermal sputtering
- Gas
  - Radiation force for Thomson opacity
  - Radiative cooling and heating
  - $\alpha$ -viscosity :  $\alpha = 0.1$

## Computational setup

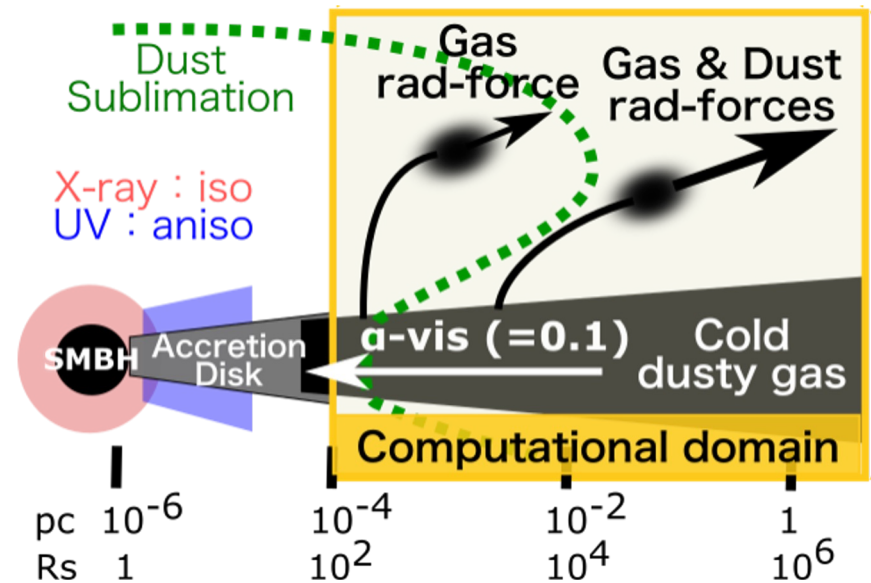
- CANS+ (Matsumoto et al. 2019)
  - Axisymmetric Cylindrical 2D( $R, z$ )
- $10^{-4}$  pc ( $10^2$  Rs)  $< R < 2$  pc,  $|z| < 2$  pc
- $\Delta R = \Delta z = 5 \times 10^{-5}$  pc = 50 Rs
- Initial Dusty disk  
with Keplerian rotation,  
and geometrically-thin cold gas

## Spatially resolved

**dust sublimation radius ( $r_{\text{sub}}$ ).**

$r < r_{\text{sub}}$  : dust-free gas

$r > r_{\text{sub}}$  : dusty gas



## AGN steady radiation sources

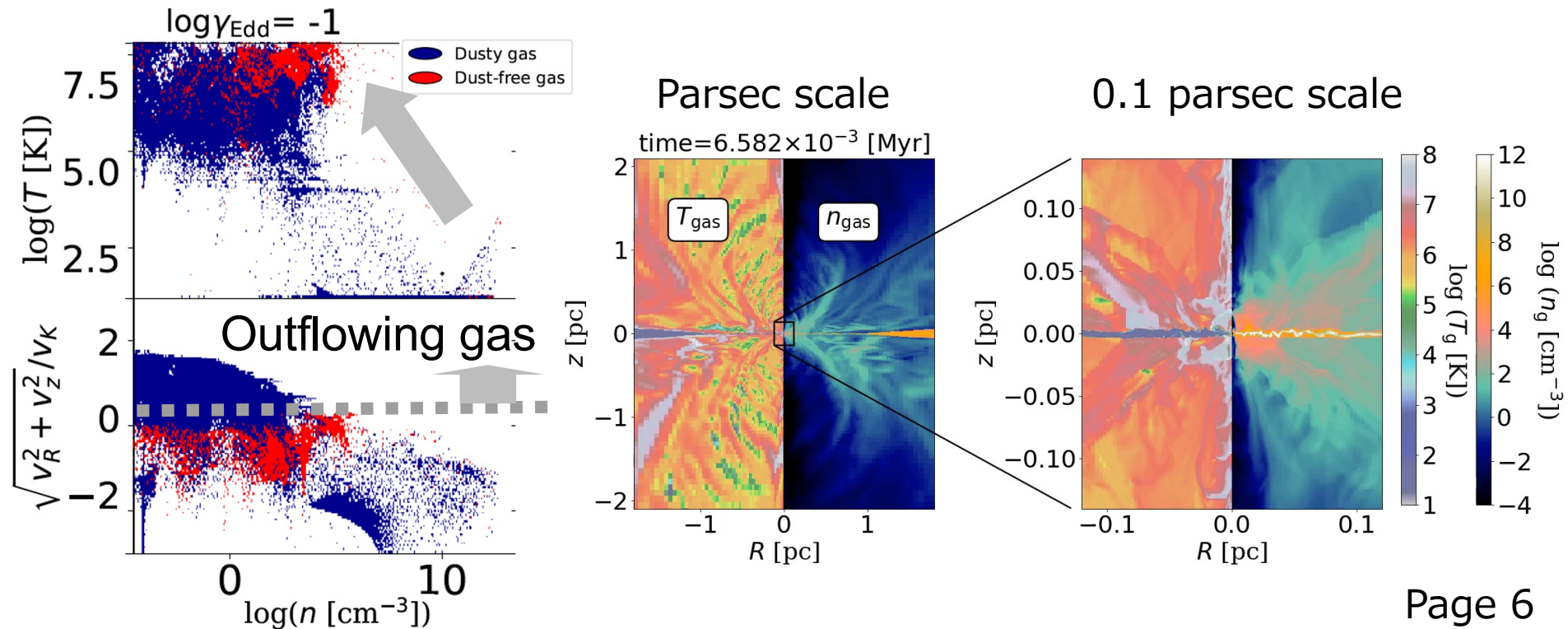
$$Y_{\text{Edd}} \propto L_{\text{bol}} / M_{\text{BH}}$$

$$Y_{\text{Edd}} = 1, 10^{-1}, 10^{-2}, 10^{-3}$$

# Multi-phase & multi-scale outflow

Case of  $\gamma_{\text{Edd}}=0.1$  (Kudoh et al. 2023)

- Propagating shells accumulate  $\rightarrow$  Torus (Wada 2012,2015)
- Radiation-driven outflow appear the shocked shells with variability.
- Inflow-induced outflow:  
 disk (low T & high  $\rho$ )  $\rightarrow$  outflow (high T & low  $\rho$ )
- **Dusty gas** can escape from the system, **dust-free gas** is bound

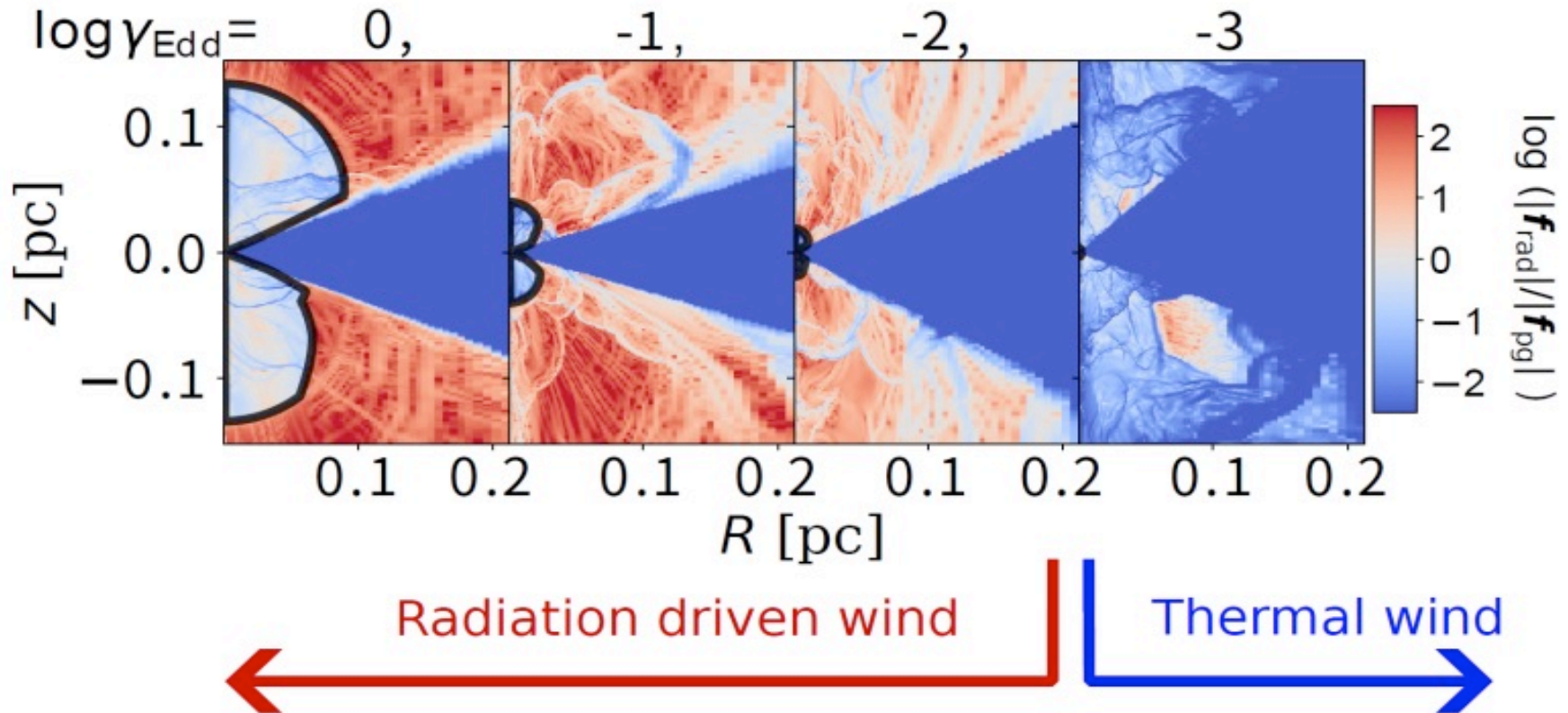


# Which is the driving mechanism: Radiation or Gas pressure?

Dependence on the Eddington ratio  $\Upsilon_{\text{Edd}} \propto L_{\text{bol}} / M_{\text{BH}}$

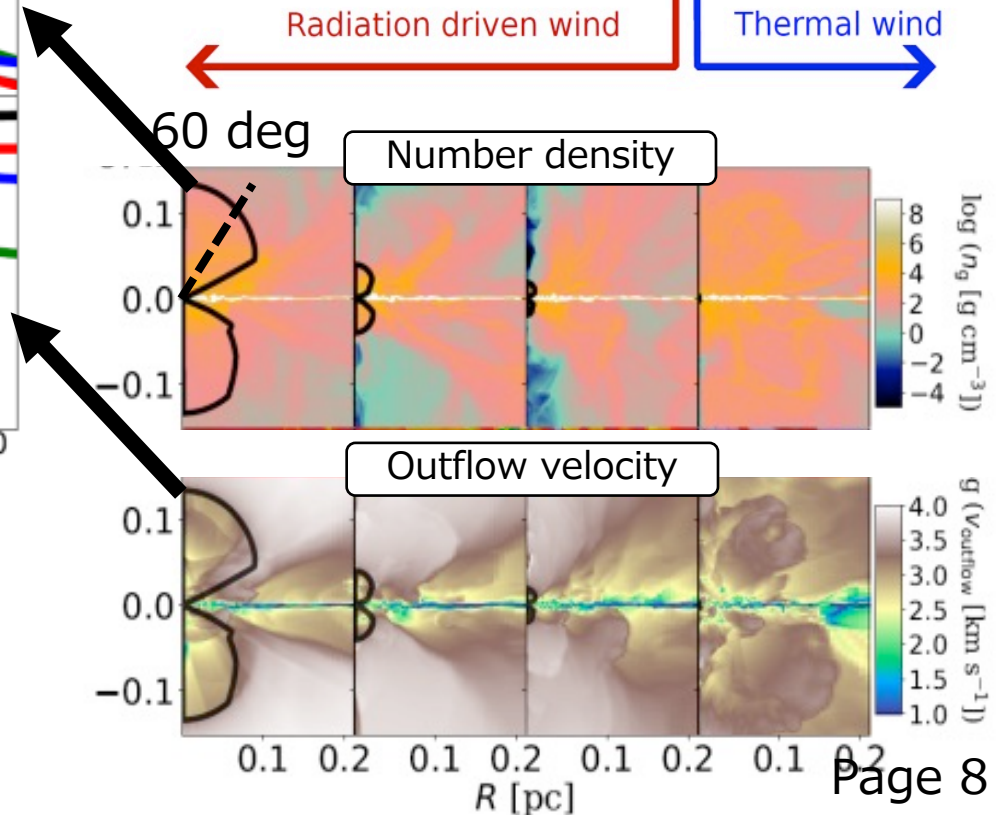
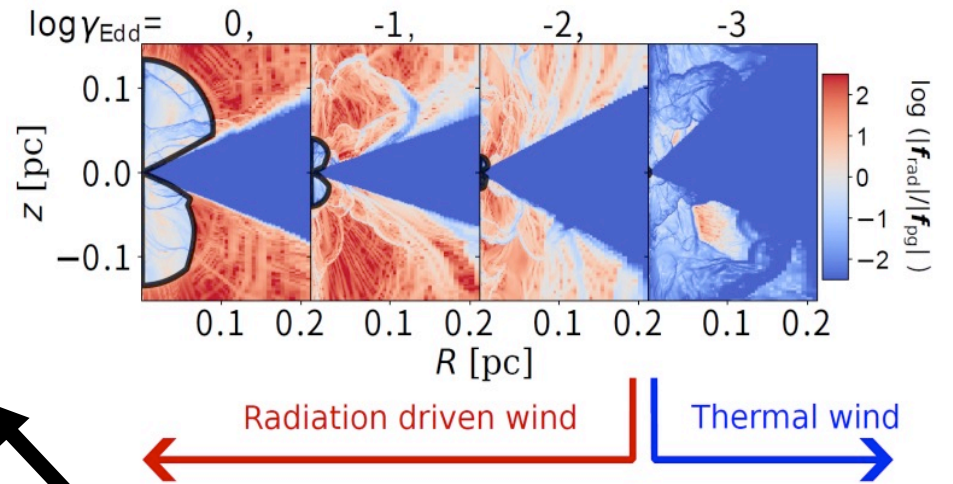
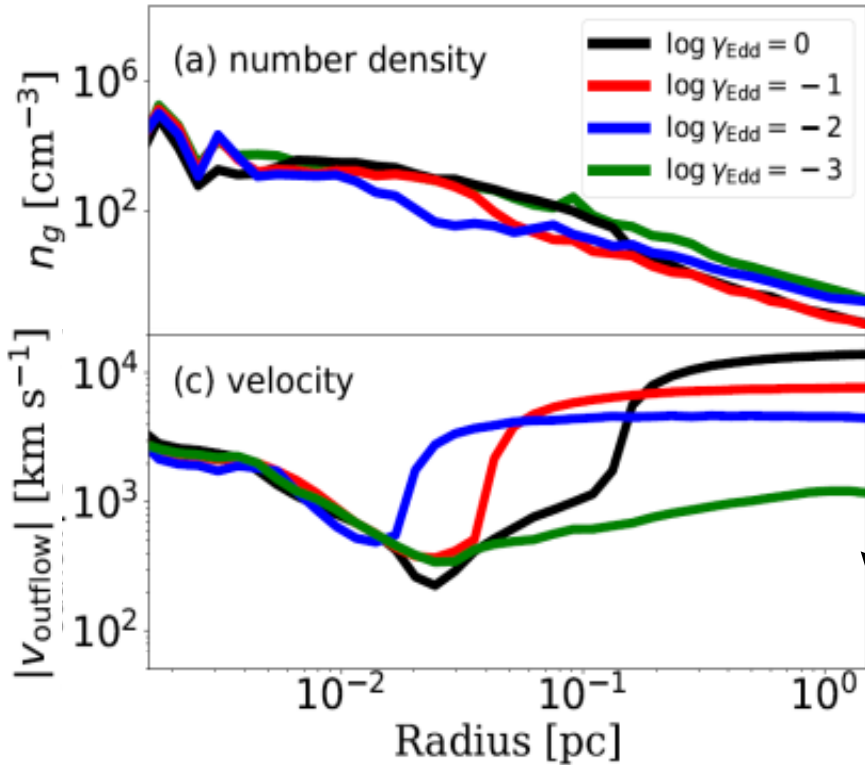
Strong radiation

Weak radiation



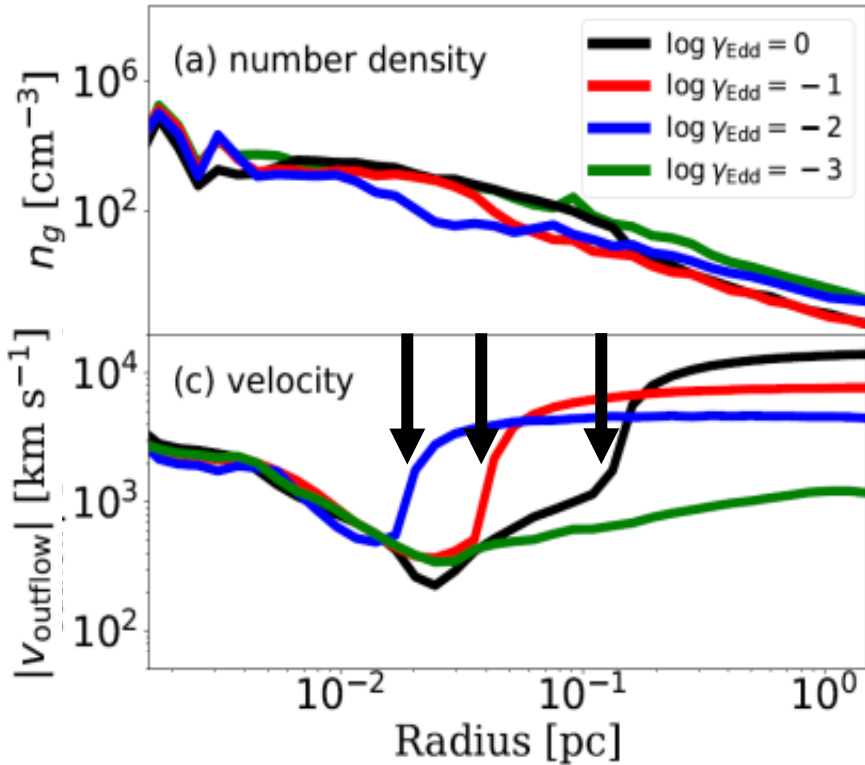
# Dynamical structure: $n$ , $v_{\text{outflow}}$

Time-averaged  
Radial profile at 60 degree

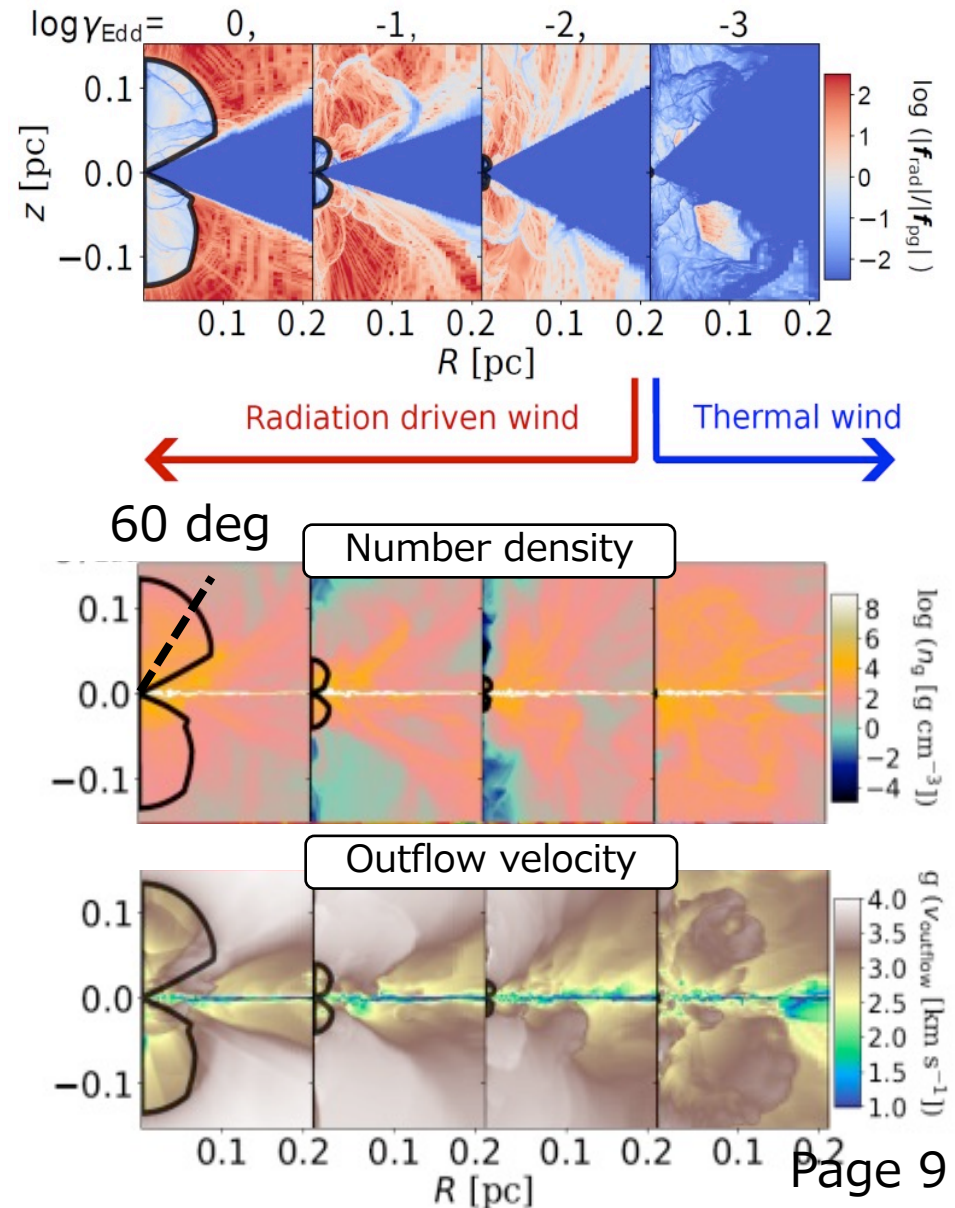


# Dynamical structure: $n$ , $v_{\text{outflow}}$

Time-averaged  
Radial profile at 60 degree

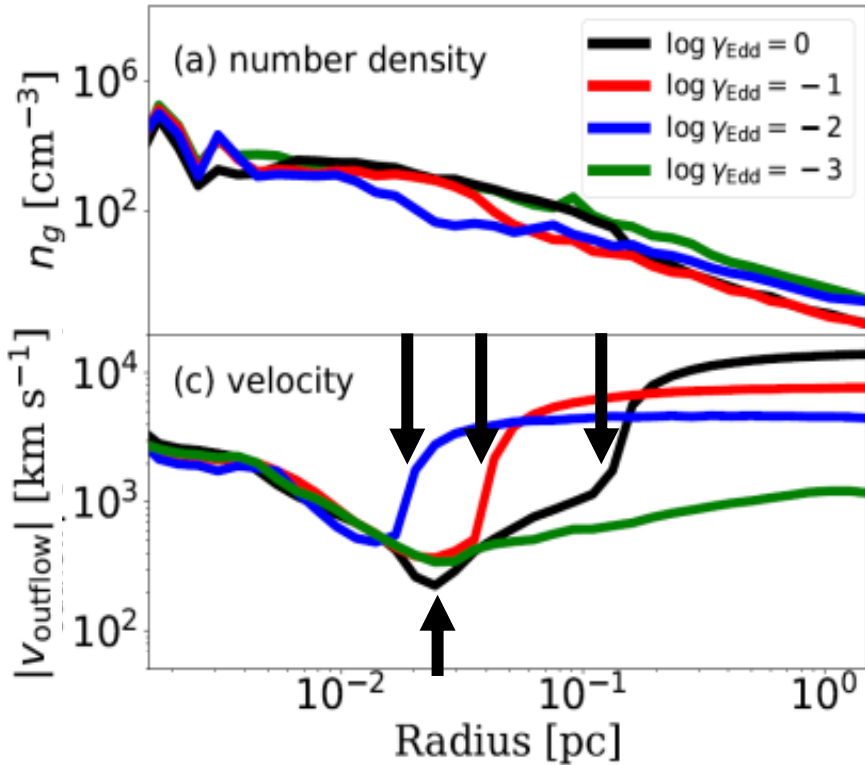


(1) Acceleration point

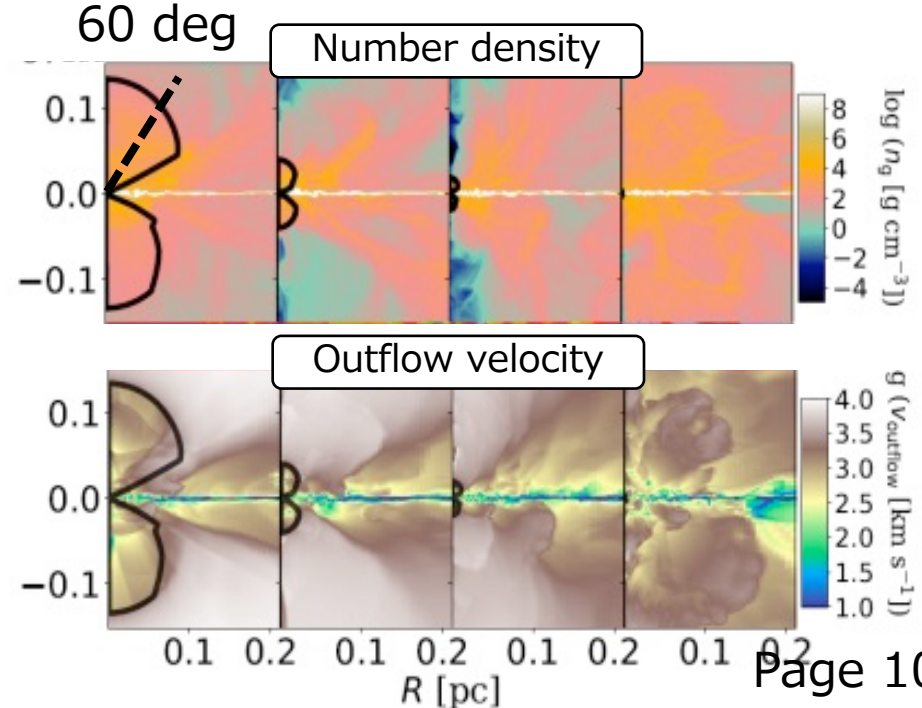
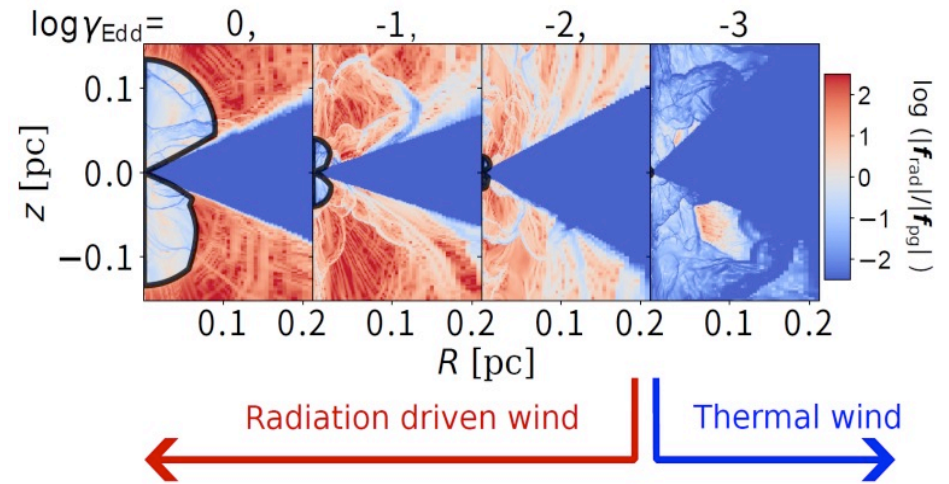


# Dynamical structure: $n$ , $v_{\text{outflow}}$

Time-averaged  
Radial profile at 60 degree

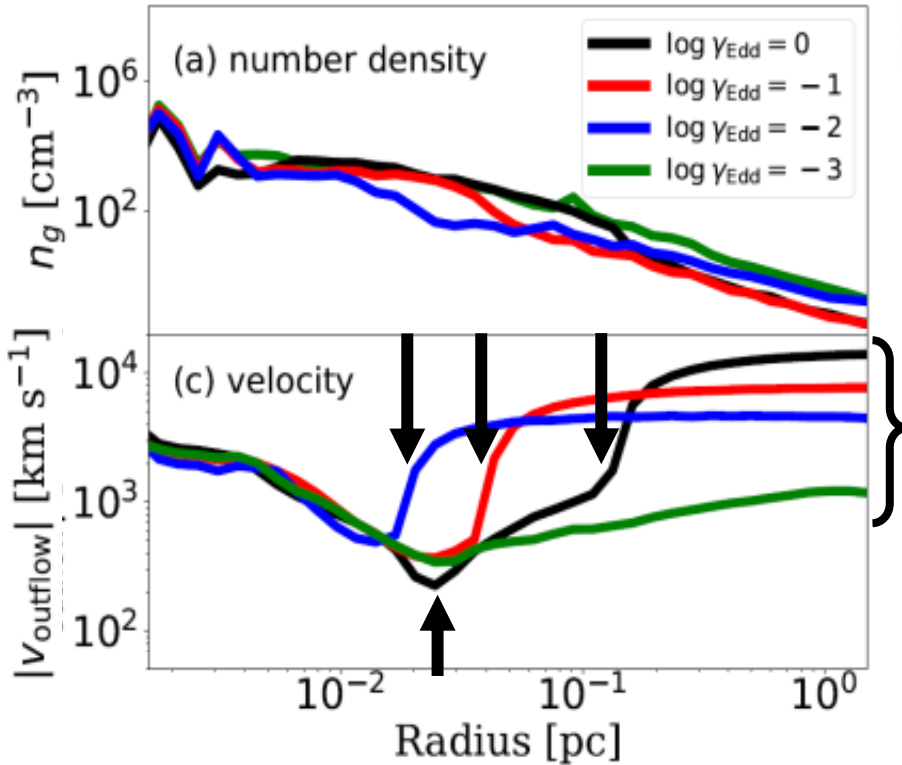


- (1) Acceleration point
- (2) Velocity Minimum

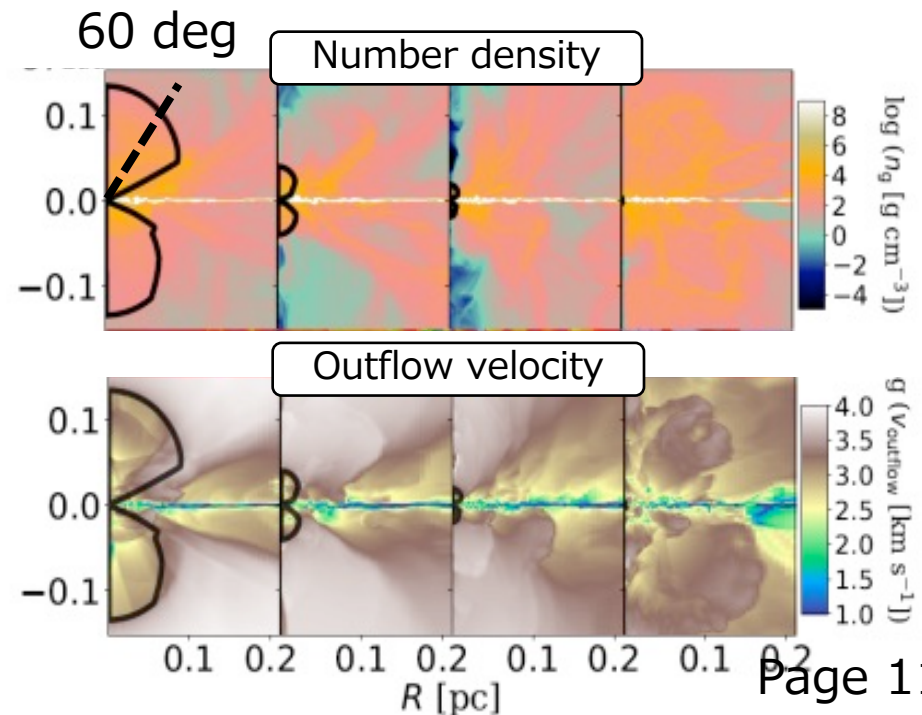
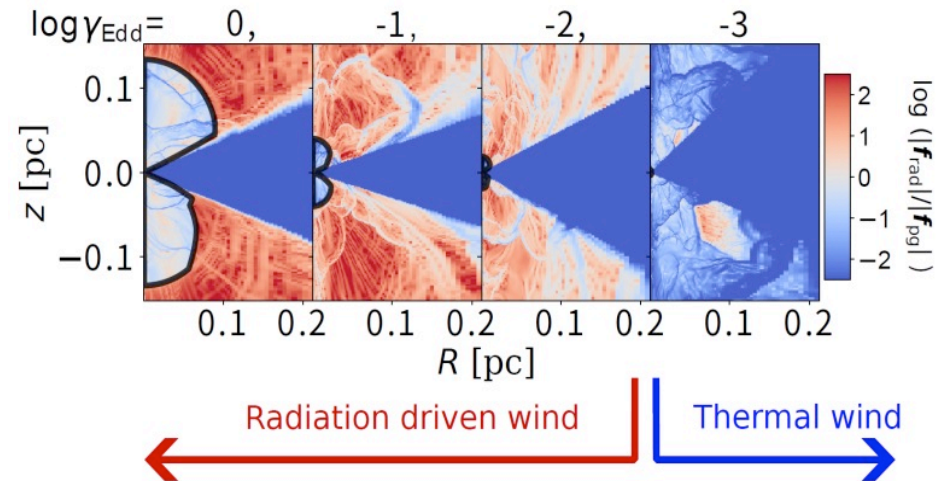


# Dynamical structure: $n$ , $v_{\text{outflow}}$

Time-averaged  
Radial profile at 60 degree



- (1) Acceleration point
- (2) Velocity Minimum
- (3) Terminal velocity



# Analytical model of outflowing shells

Equation of motion **radiation** + gravity + **gas pressure** (isothermal)

$$\frac{dv(r)}{dt} = \left( \frac{\kappa L}{c 4\pi} - \frac{GM_{\text{SMBH}}}{r^2} \right) + \frac{c_s^2}{\gamma p} \frac{dp}{dr} \quad d/dr \sim r^{-1}$$

$$\frac{dv(r)}{dt} \sim (\Gamma_{\text{Edd}} - 1) \frac{r_g}{r} \frac{c^2}{2r} + \frac{c_s^2}{\gamma r}$$

Solutions for outflow velocity

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + (\Gamma_{\text{Edd}} - 1) \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)$$

Force ratio of radiation to gravity

**Dusty gas**  $\Gamma_{\text{Edd,d}} = \frac{\kappa}{\kappa_{\text{T}}} \delta_L \gamma_{\text{Edd}}$

**Dust-free gas**  $\Gamma_{\text{Edd,g}} = \delta_L \gamma_{\text{Edd}}$

$$\Upsilon_{\text{Edd}} \propto L_{\text{bol}} / M_{\text{BH}}$$

$$r_g = 2GM_{\text{SMBH}}/c^2 \sim 10^{-6} \text{ pc } (M_{\text{SMBH}}/10^7 M_{\odot})$$

# Dynamical structure ( $\log \gamma_{\text{Edd}} = 0$ )

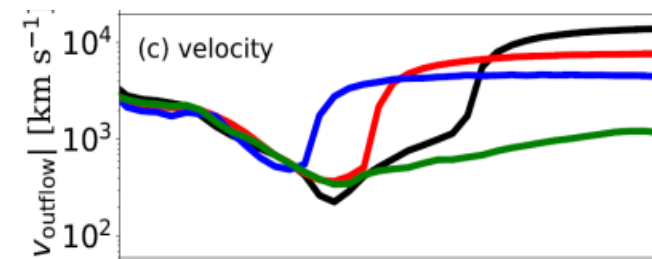
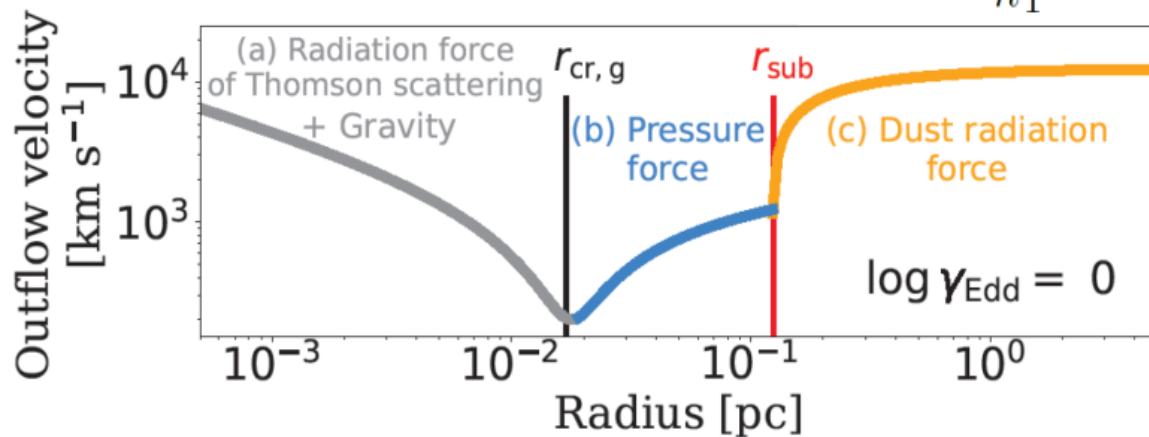
Analytic solution

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + \underbrace{(\Gamma_{\text{Edd}} - 1)}_{\text{radiation}} \underbrace{\left( \frac{r_g}{r_0} \right)}_{\text{gravity}} \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \underbrace{\frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)}_{\text{gas pressure}}$$

**Dust-free gas**

**Dusty gas**

$$\Gamma_{\text{Edd,g}} = \delta_L \gamma_{\text{Edd}} \quad \downarrow \quad \Gamma_{\text{Edd,d}} = \frac{\kappa}{\kappa_T} \delta_L \gamma_{\text{Edd}}$$



- (1) Acceleration point
- (2) Velocity Minimum
- (3) Terminal velocity

Critical point ( $dv/dt = 0$ )

$$r_{\text{cr}} = (1 - \Gamma_{\text{Edd}}) \frac{\gamma}{2} \left( \frac{c}{c_s} \right)^2 r_g$$

$$= 0.017 \text{ pc} (1 - \Gamma_{\text{Edd},i}) \left( \frac{c/c_s}{200} \right)^2 \left( \frac{M_{\text{SMBH}}}{10^7 M_\odot} \right)$$

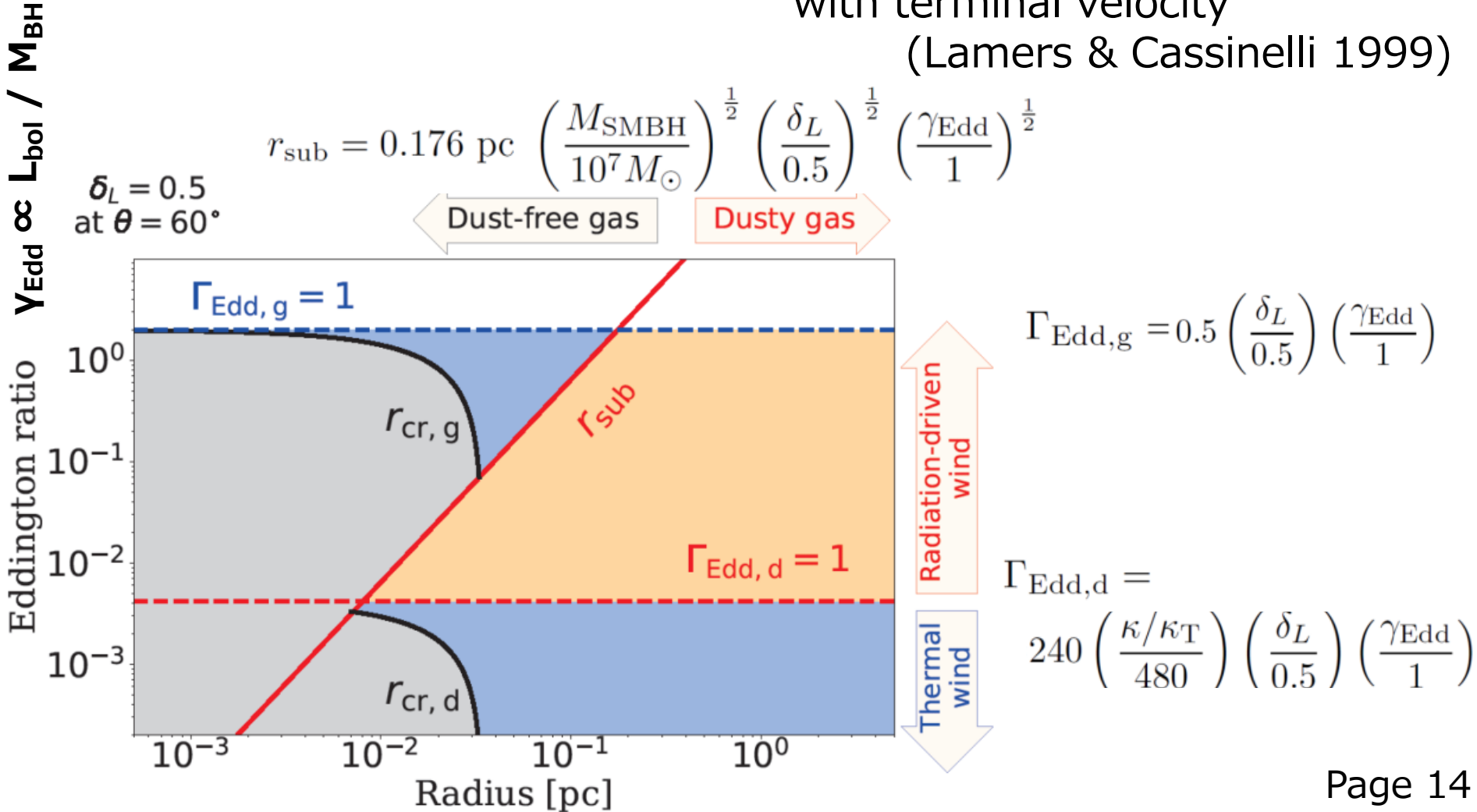
Dust sublimation radius

$$r_{\text{sub}} = \sqrt{\frac{\delta_L L_{\text{bol}}}{4\pi\sigma_{\text{SB}} T_d^4}}$$

$$= 0.176 \text{ pc} \left( \frac{M_{\text{SMBH}}}{10^7 M_\odot} \right)^{\frac{1}{2}} \left( \frac{\delta_L}{0.5} \right)^{\frac{1}{2}} \left( \frac{\gamma_{\text{Edd}}}{1} \right)^{\frac{1}{2}} \left( \frac{T_d}{1500 \text{ K}} \right)^{-2}$$

# Dynamical structure

- Domain (a) gravity
  - (b) gas pressure
  - (c) dust radiation force
- } → Solar wind solution (Parker 1960)  
 → Dusty stellar wind solution with terminal velocity (Lamers & Cassinelli 1999)



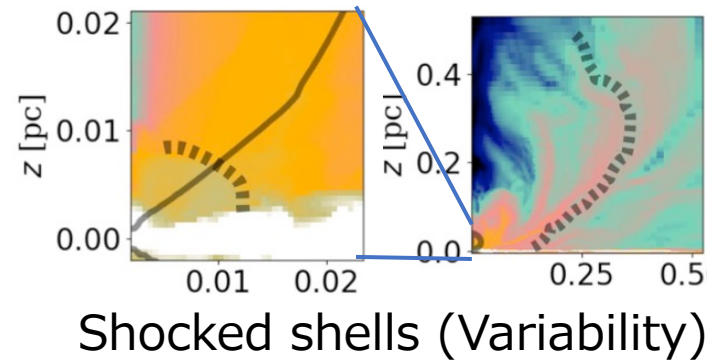
# Summary

- We investigated the dependence of the Eddington ratio on sub-pc-scale outflows using axisymmetric 2D simulations.

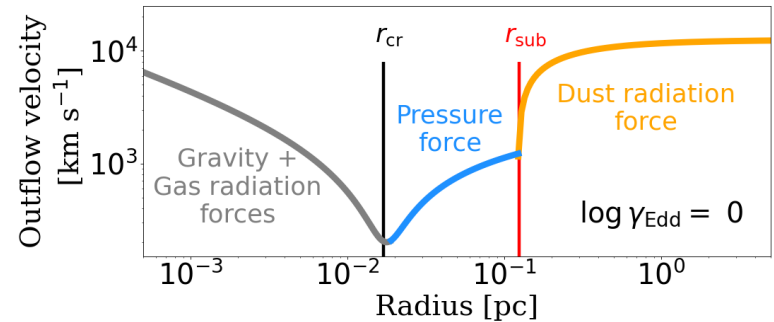
- **Outflowing shells with variability** are described as the **analytic solutions of steady**.

- Dusty wind activated on when Eddington ratio  $> -3$ .

- Important parameters are  $r > r_{\text{sub}}$  and  $\Gamma_{\text{Edd,d}} > 1$ .



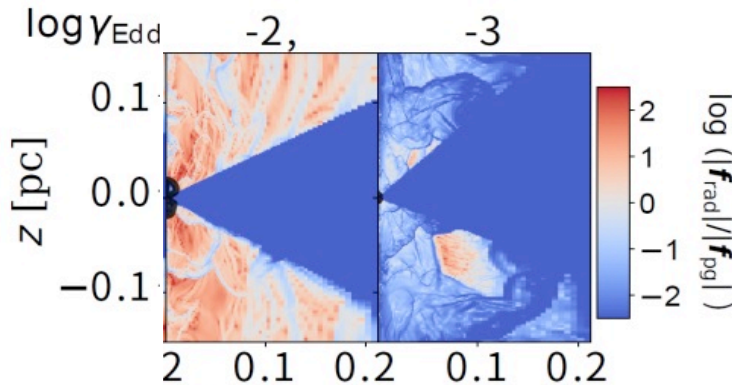
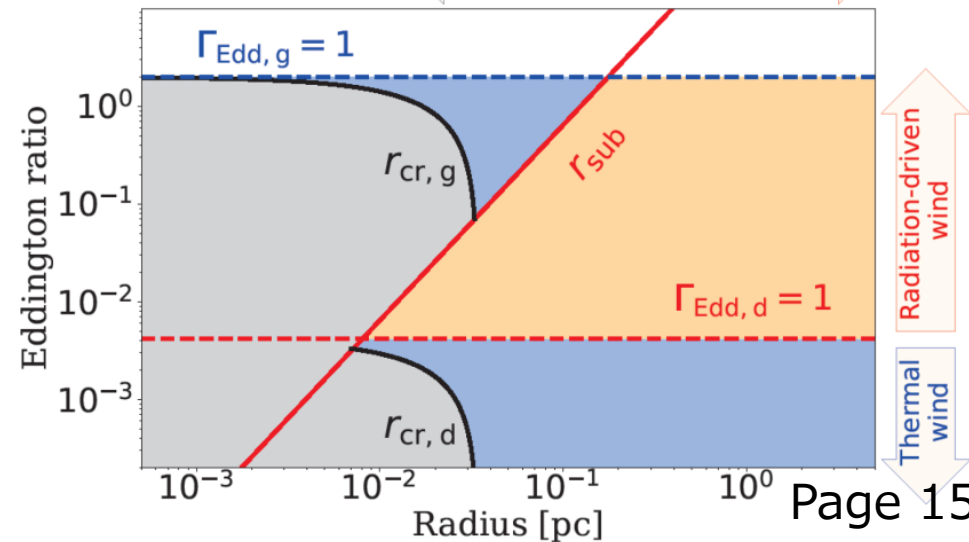
Wind solution (Time-averaged)



$\delta_L = 0.5$   
at  $\theta = 60^\circ$

Dust-free gas

Dusty gas

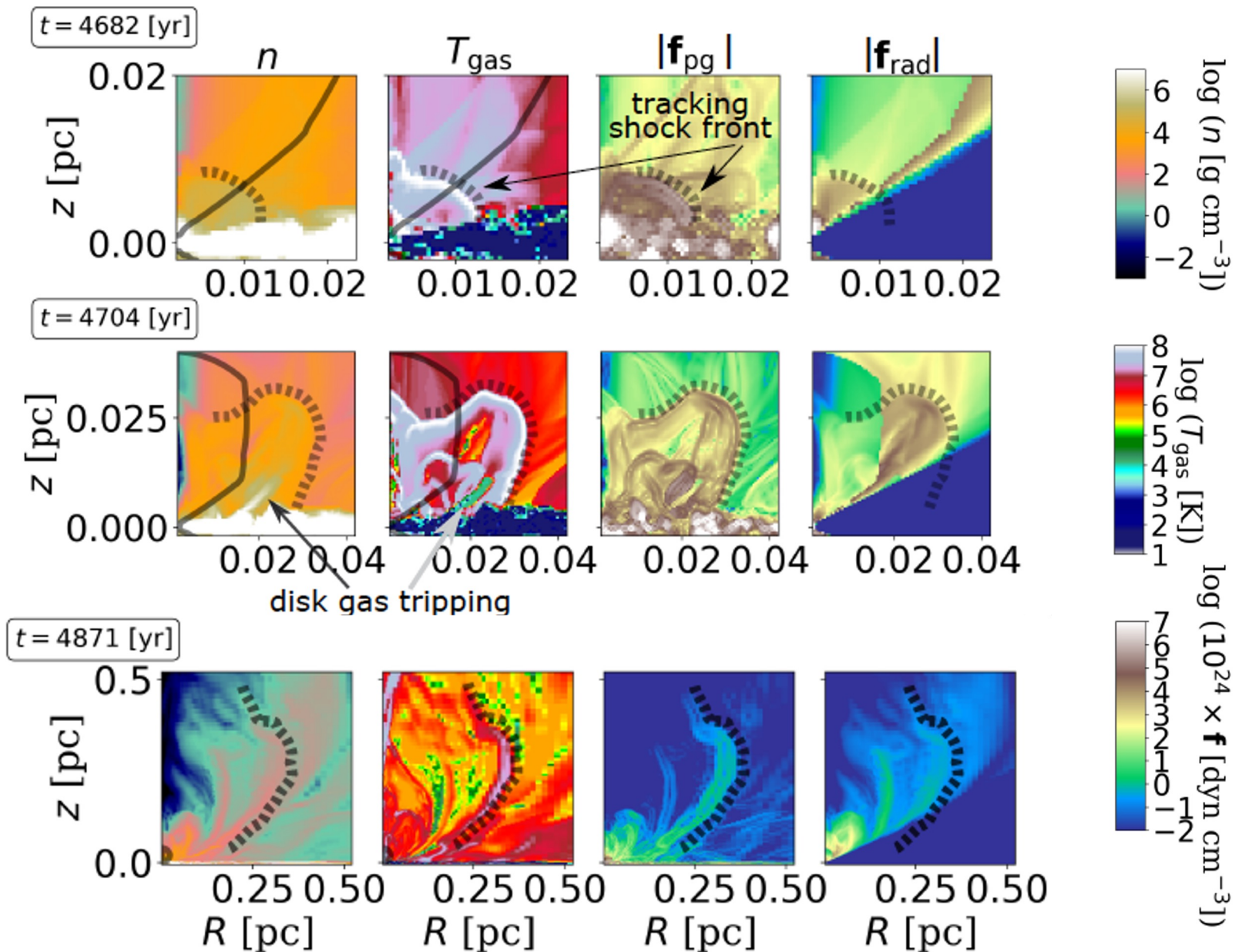


Radiation driven wind

Thermal wind



# Shell propagation with shock



# Gas-dust radiation hydrodynamic equations

- Mass conservation (dust & gas)

$$\frac{\partial \rho}{\partial t} + \nabla \cdot [\rho \mathbf{v}] = 0 \quad \rho = \rho_{\text{gas}} + \rho_{\text{dust}} \sim \rho_{\text{gas}} \quad \frac{\rho_{\text{dust}}}{\rho_{\text{gas}}} = \text{const.}$$

dust-to-gas mass ratio

Sublimation :  $T_{\text{dust}} > 1500 \text{ K}$ ,  $r_{\text{sub}} \sim 0.01 \text{ pc}$  @  $a = 0.01 \mu\text{m}$

Sputtering :  $t_{\text{sput}} < \Delta t_{\text{hydro}}$  @  $a = 0.01 \mu\text{m}$

- Momentum conservation  $O(v/c)$

$$\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot [\rho \mathbf{v} \mathbf{v} + P_g \mathbf{I}] = \mathbf{f}_{\text{rad}} + \mathbf{f}_{\text{grav}} + \mathbf{f}_{\text{vis}} \quad \mathbf{f}_{\text{rad}} = \int_{10^{10} \text{ Hz}}^{10^{20} \text{ Hz}} \frac{(\rho_d \kappa_{d,\nu} + \rho_g \kappa_T)}{c} F_\nu \mathbf{e}_r d\nu$$

Radiation force

- Energy conservation

$$\frac{\partial e}{\partial t} + \nabla \cdot [(e + P_g) \mathbf{v}] = -\rho \mathcal{L} + \mathbf{v} \cdot \mathbf{f}_{\text{rad}} + \mathbf{v} \cdot \mathbf{f}_{\text{grav}} + W_{\text{vis}}$$

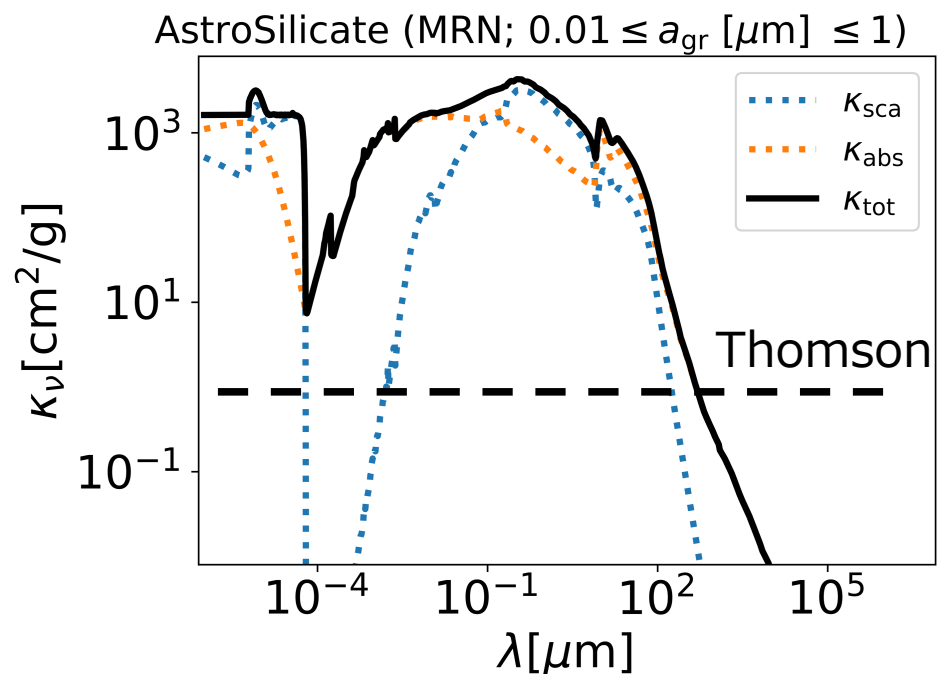
Cooling/Heating    Work for rad-force



We solve the gas-dust centroid system.

# Dust model

Dust opacity (astroSilicate; Draine 2003)



Dust radiation force

$$f_{\text{rad}} = \int_{10^{10}\text{Hz}}^{10^{20}\text{Hz}} \frac{(\rho_d \kappa_{d,\nu} + \rho_g \kappa_T)}{c} F_\nu e_\tau d\nu$$

Opacity
Radiation flux

Size distribution: MRN model

$0.01 < a < 1 \mu\text{m}$

(Mathis et al. 1977, Drain & Lee 1984)

$$n(a)da = A n_H a^{-\beta} da \quad \beta = -3.5$$

Dust destruction

- Sublimation

(Namekata et al. 2016

Chan and Krolic 2017)

- Sputtering

(Tasai and Mathews 1995)

$$\int \frac{L_\nu e^{-\tau_\nu}}{4\pi r^2} \kappa_{d,\nu}(a) \frac{4\pi}{3} a^3 \rho_{\text{grain}} n(a) dv da - \int 4\pi B_\nu(T_d) \kappa_{d,\nu}(a) \frac{4\pi}{3} a^3 \rho_{\text{grain}} n(a) dv da = 0,$$

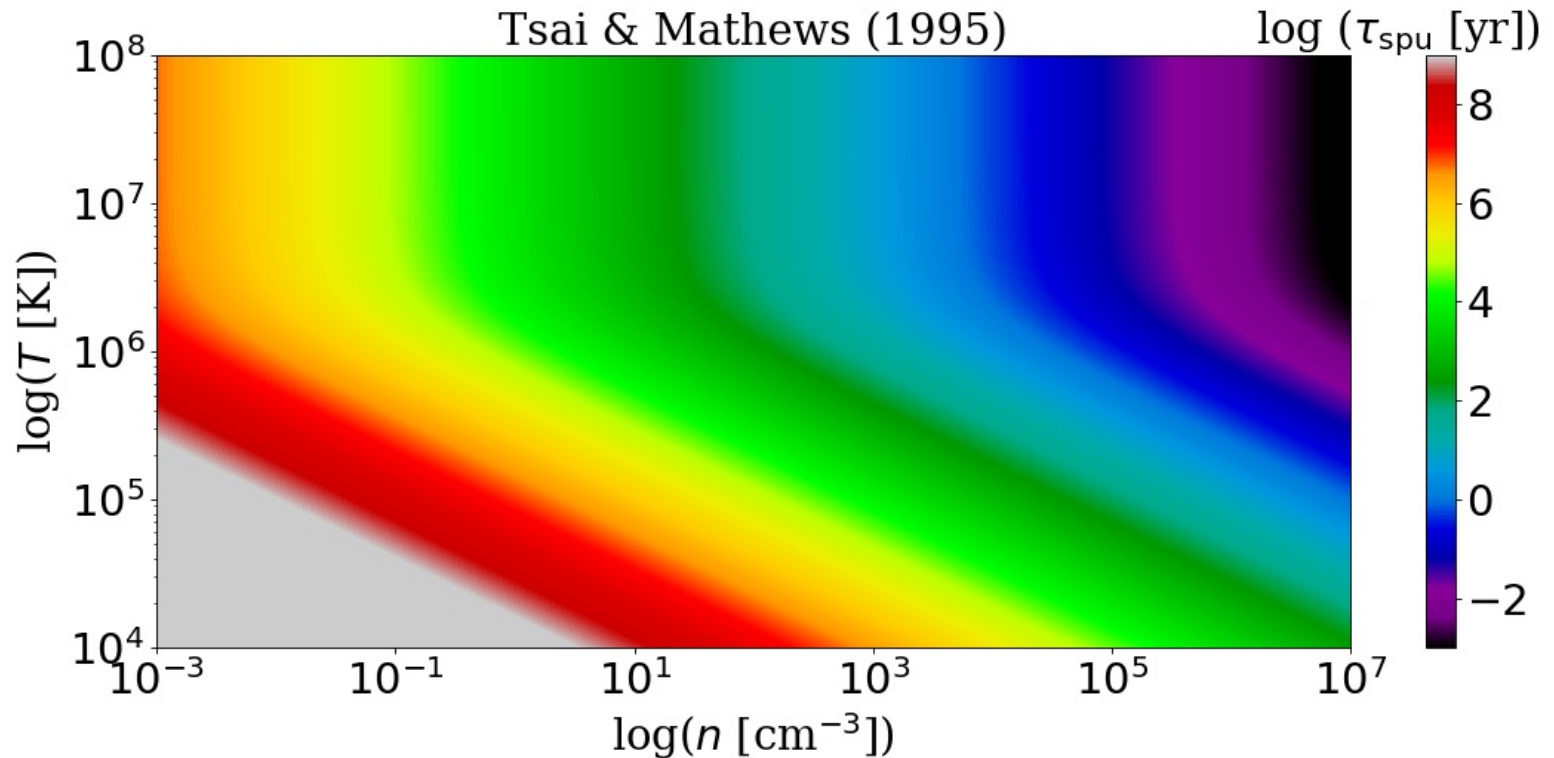
$$T_{\text{dust}} > 1500 \text{ K}, \quad t_{\text{spu}} < \Delta t_{\text{hydro}}$$

$$\tau_{\text{sp}} = 5.5 \times 10^3 \text{ yr} \left( \frac{n}{1 \text{ cm}^{-3}} \right)^{-1} \left( \frac{a}{0.01 \mu\text{m}} \right) \left[ \left( \frac{2 \times 10^6}{T} \right)^{2.5} + 1 \right]$$

# Dust destruction processes

Dust sputtering (collisional)

$$\tau_{\text{sp}} = 5.5 \times 10^3 \text{ yr} \left( \frac{n}{1 \text{ cm}^{-3}} \right)^{-1} \left( \frac{a}{0.01 \text{ } \mu\text{m}} \right) \left[ \left( \frac{2 \times 10^6}{T} \right)^{2.5} + 1 \right]$$



# Simulation setup

Dusty outflow in Eddington ratio 0.1

**Physics** (Wada 2012, 2015)

- Dust-radiation-hydrodynamic equation
- SMBH gravity  $M_{\text{BH}} = 10^7 M_{\odot}$
- Dust

**AGN steady radiation field**

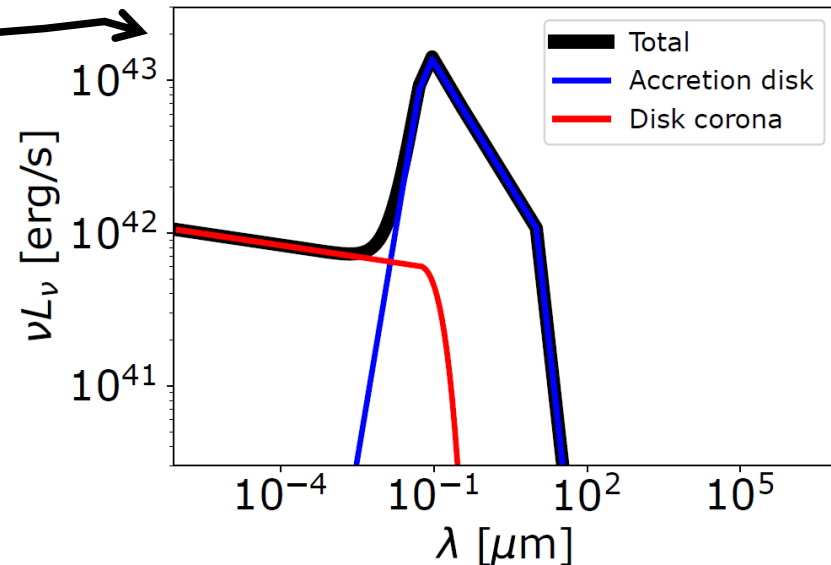
- Eddington ratio  $\gamma_{\text{Edd}} = 0.1$

Eddington luminosity (Given)

$$L_{\text{Edd}} = 1.41 \times 10^{45} \left( \frac{M_{\text{BH}}}{10^7 M_{\odot}} \right) \text{ erg/s}$$

Eddington ratio  $\gamma_{\text{Edd}} \equiv \frac{L_{\text{bol}}}{L_{\text{Edd}}} = 0.1$   
(Given)

Generate AGN SED



# Simulation model

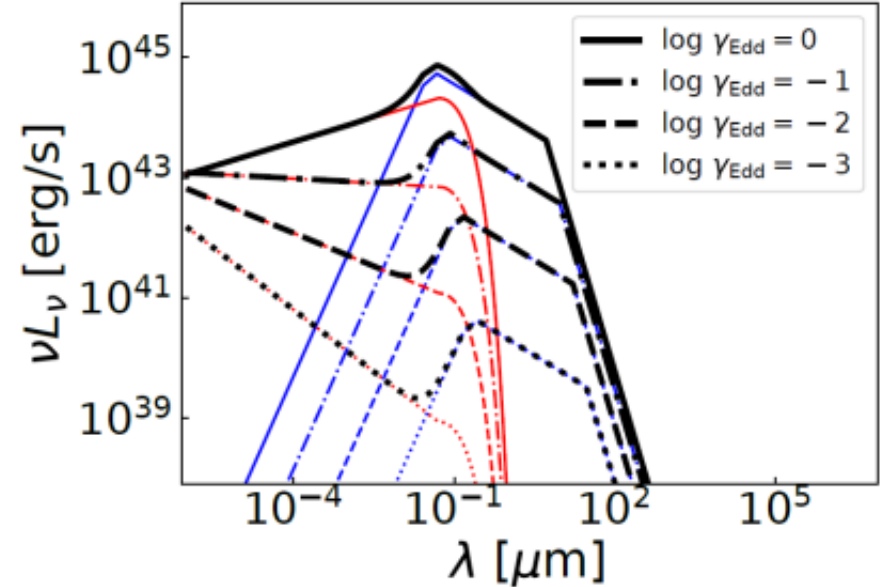
## Physics (Kudoh et al. 2023)

- Dust-radiation-hydrodynamic equation
- SMBH gravity
- Dust
  - $M_{\text{BH}} = 10^7 M_{\odot}$
  - Dust-gas mass ratio = 0.01
  - Radiation force for dust opacity
  - Dust destruction : sublimation, sputtering
- Gas
  - Radiation force for Thomson opacity
  - Radiative cooling and heating
  - $\alpha$ -viscosity :  $\alpha = 0.1$

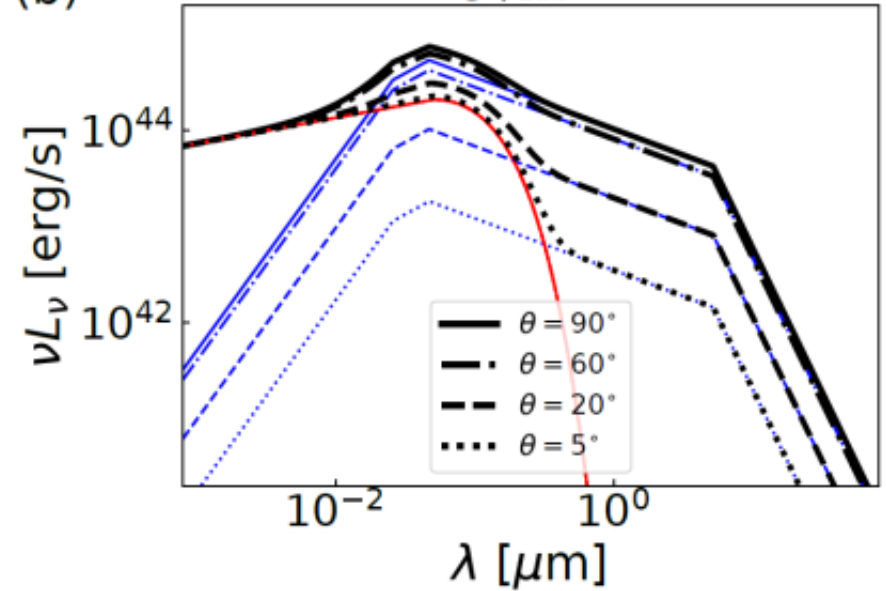
## Computational setup

- CANS+ (Matsumoto et al. 2019)
- Axisymmetric Cylindrical 2D(R, z)
- $10^{-4} \text{ pc} (10^2 R_s) < R < 2 \text{ pc}, |z| < 2 \text{ pc}$
- $\Delta R = \Delta z = 5 \times 10^{-5} \text{ pc} = 50 R_s$
- Initial Dusty disk
  - with Keplerian rotation,
  - and geometrically-thin cold gas

(a)  $M_{\text{SMBH}} = 10^7 M_{\odot}, L_{\text{Edd}} = 1.25 \times 10^{45} \text{ [erg/s]}$



(b)  $\log \gamma_{\text{Edd}} = 0$

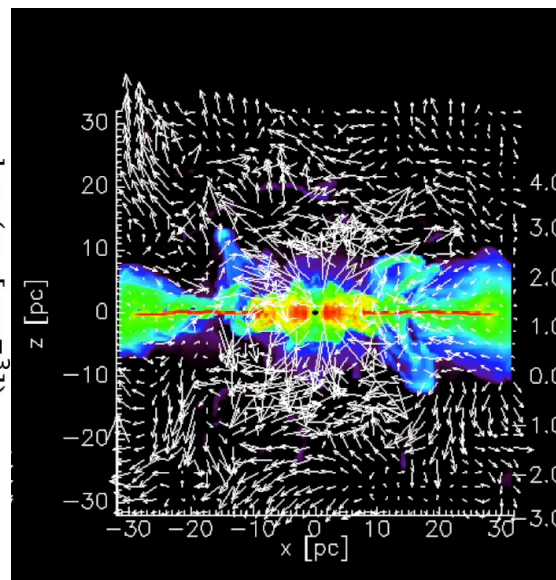
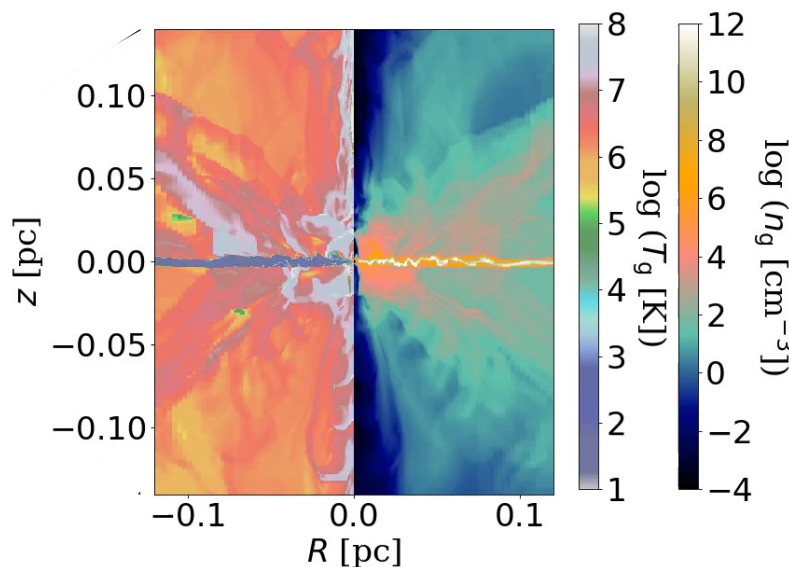


# Ionized Dusty Outflow: Simulation

The torus is an accumulation of dusty outflow.

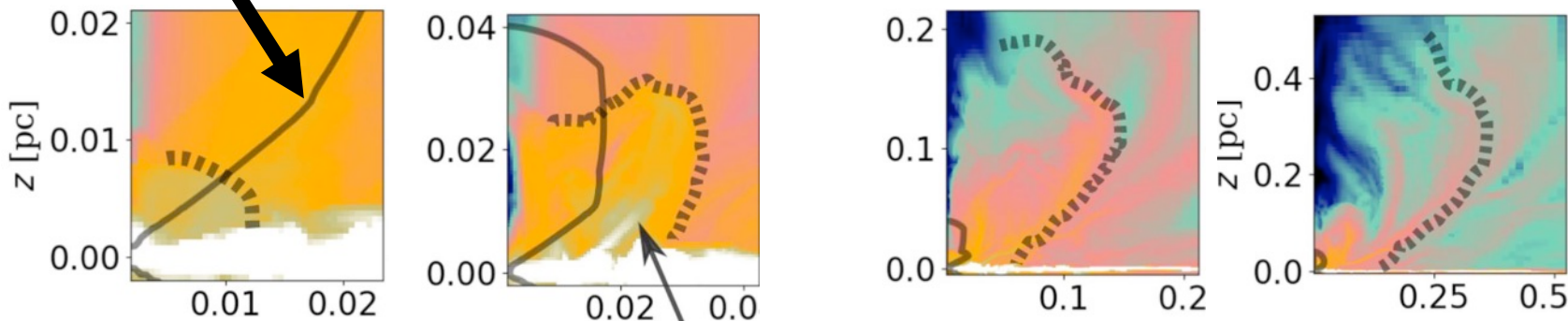
Sub-pc-scale: Kudoh et al. 2023

Ten-pc-scale: Wada 2015



Dust sublimation radius ( $r_{\text{sub}}$ )

Shocked shell propagation



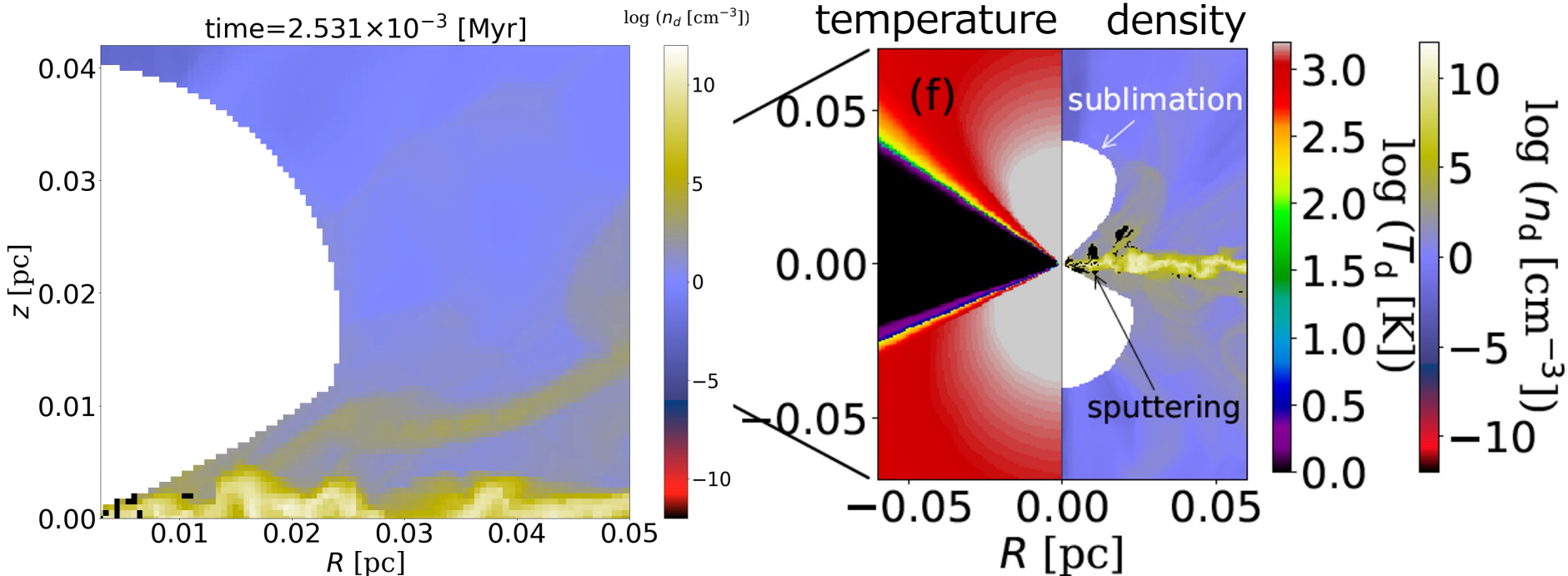
# Dust distribution

- Dust density: Shape of dust sublimation region has time-variability.
- Dust temperature:  
Around mid-plane, cold dust appear due to attenuation by outflow.

Dust density distribution

White: dust sublimation region,

Black : dust sputtering region.



# Velocity field & Force ratio

## Where outflow are accelerated?

Inside the dust sublimation region,  
gas is gravitationally bound and gas pressure are dominated.

A part of gas lifted by the gas pressure  
is accelerated by dust radiation force.

- Velocity arrows

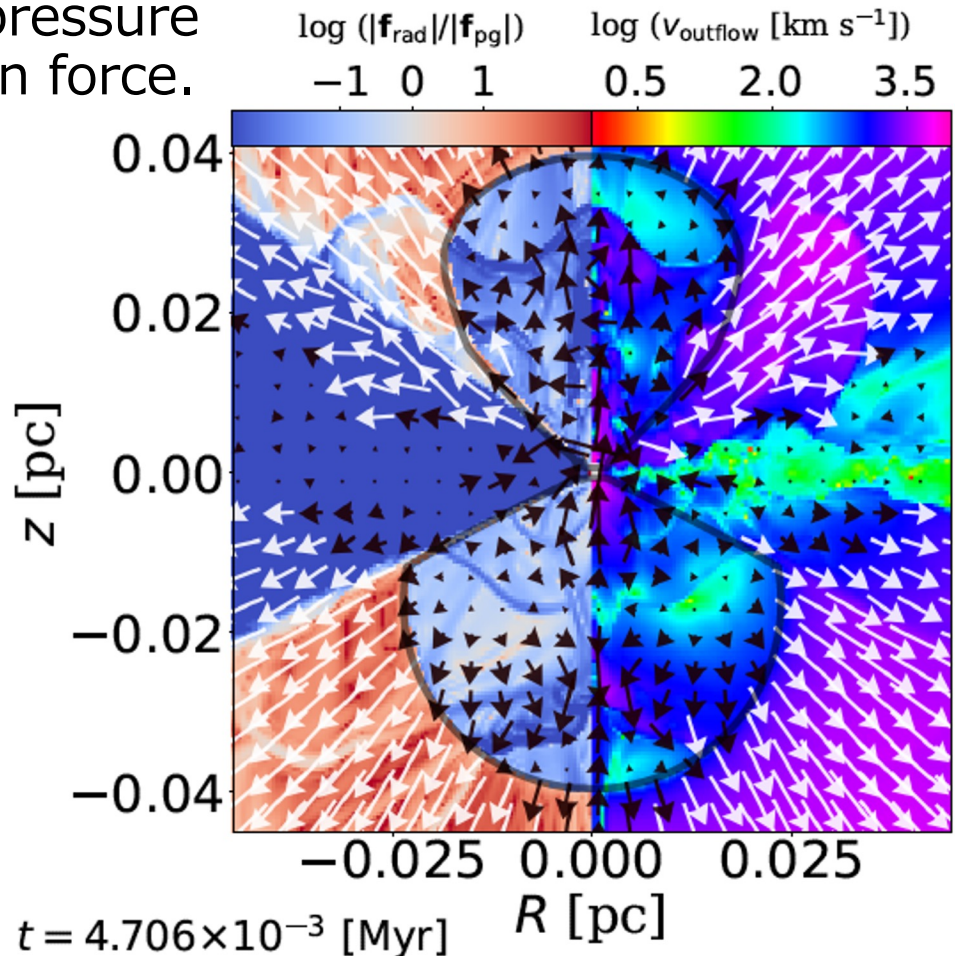
White: gas escapable  
Black: gravitationally bound

- Left hand side

Red : Radiation force  
Blue : Gas pressure force

- Right hand side

Magnitude of poloidal velocity



# Dynamical structure ( $\log \Upsilon_{\text{Edd}} = 0$ )

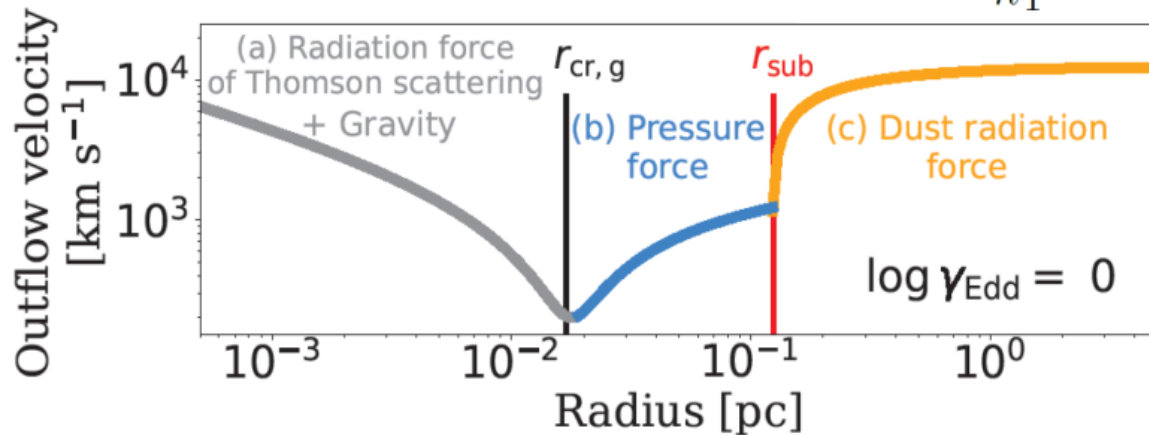
Analytic solution

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + \underbrace{(\Gamma_{\text{Edd}} - 1)}_{\text{radiation}} \underbrace{\left( \frac{r_g}{r_0} \right)}_{\text{gravity}} \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \underbrace{\frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)}_{\text{gas pressure}}$$

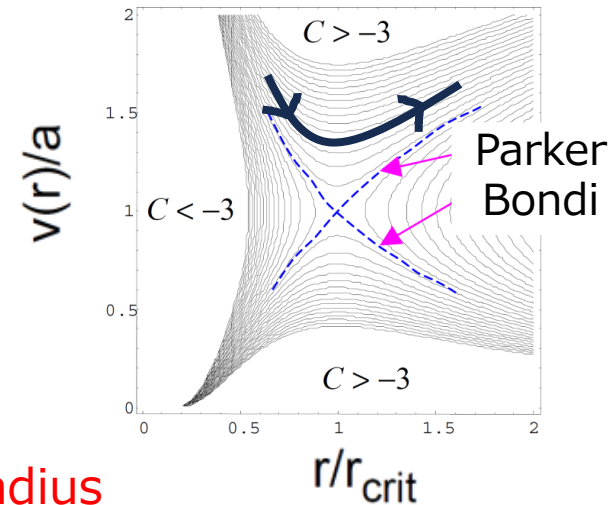
**Dust-free gas**

**Dusty gas**

$$\Gamma_{\text{Edd,g}} = \delta_L \gamma_{\text{Edd}} \quad \downarrow \quad \Gamma_{\text{Edd,d}} = \frac{\kappa}{\kappa_T} \delta_L \gamma_{\text{Edd}}$$



Steady stellar/solar wind



Critical point (dv/dt = 0)

$$r_{\text{cr}} = (1 - \Gamma_{\text{Edd}}) \frac{\gamma}{2} \left( \frac{c}{c_s} \right)^2 r_g$$

$$= 0.017 \text{ pc} (1 - \Gamma_{\text{Edd},i}) \left( \frac{c/c_s}{200} \right)^2 \left( \frac{M_{\text{SMBH}}}{10^7 M_\odot} \right)$$

Dust sublimation radius

$$r_{\text{sub}} = \sqrt{\frac{\delta_L L_{\text{bol}}}{4\pi\sigma_{\text{SB}} T_d^4}}$$

$$= 0.176 \text{ pc} \left( \frac{M_{\text{SMBH}}}{10^7 M_\odot} \right)^{\frac{1}{2}} \left( \frac{\delta_L}{0.5} \right)^{\frac{1}{2}} \left( \frac{\gamma_{\text{Edd}}}{1} \right)^{\frac{1}{2}} \left( \frac{T_d}{1500 \text{ K}} \right)^{-2}$$

# Dynamical structure ( $\log \Upsilon_{\text{Edd}} = 0$ )

Analytic solution

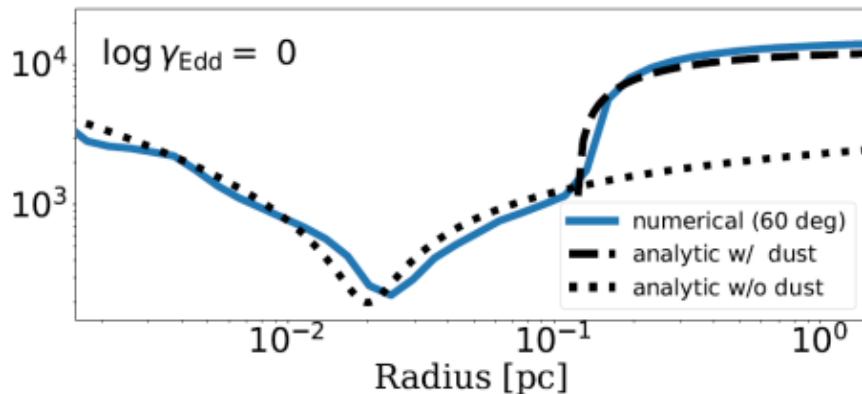
$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + \underbrace{(\Gamma_{\text{Edd}} - 1)}_{\text{radiation}} \underbrace{\left( \frac{r_g}{r_0} \right)}_{\text{gravity}} \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \underbrace{\frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)}_{\text{gas pressure}}$$

Numerical solutions vs Analytic solutions

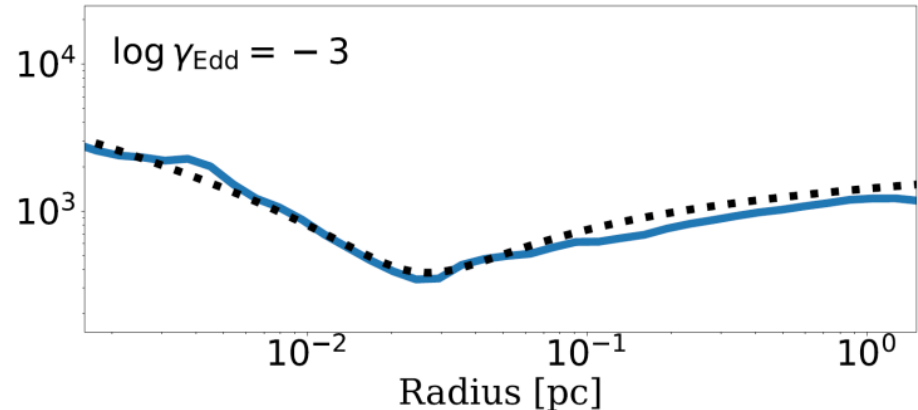
Dotted lines : Dust-free gas

Dashed line : Dusty gas

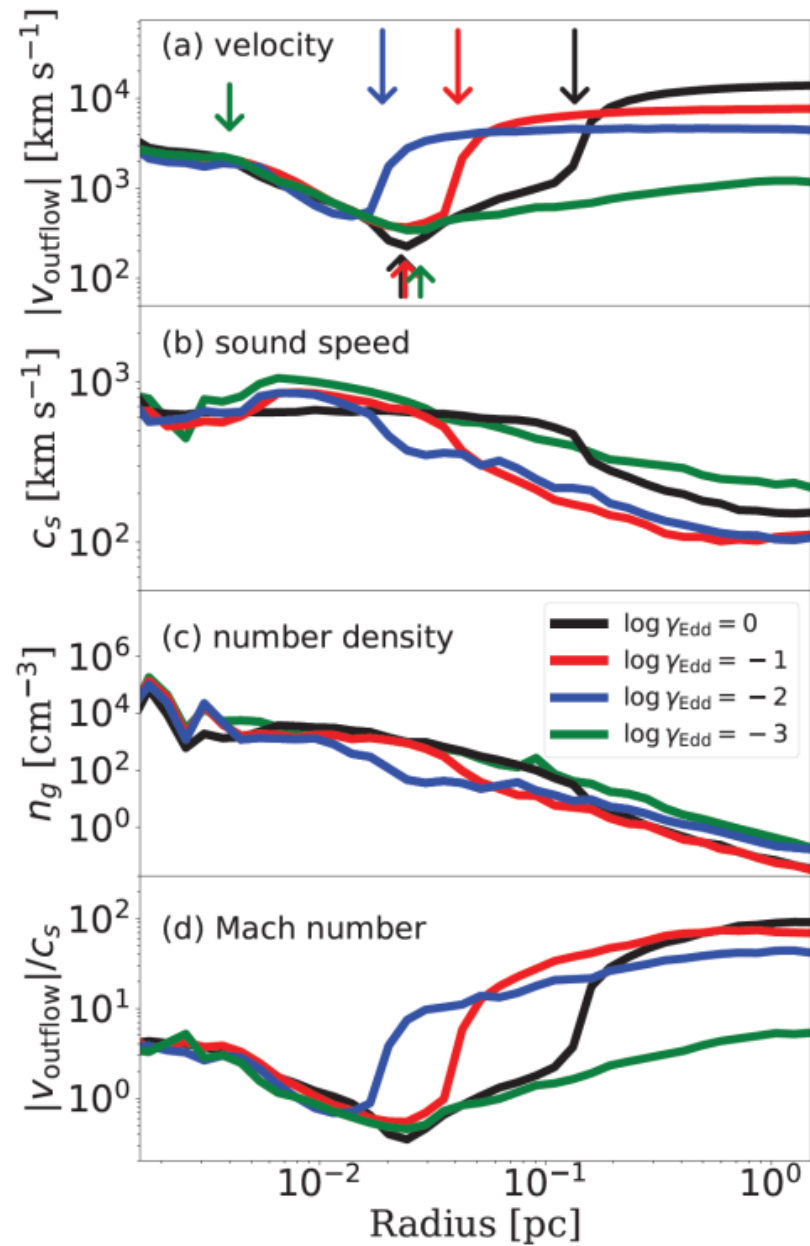
Radiation driven wind



Thermal wind



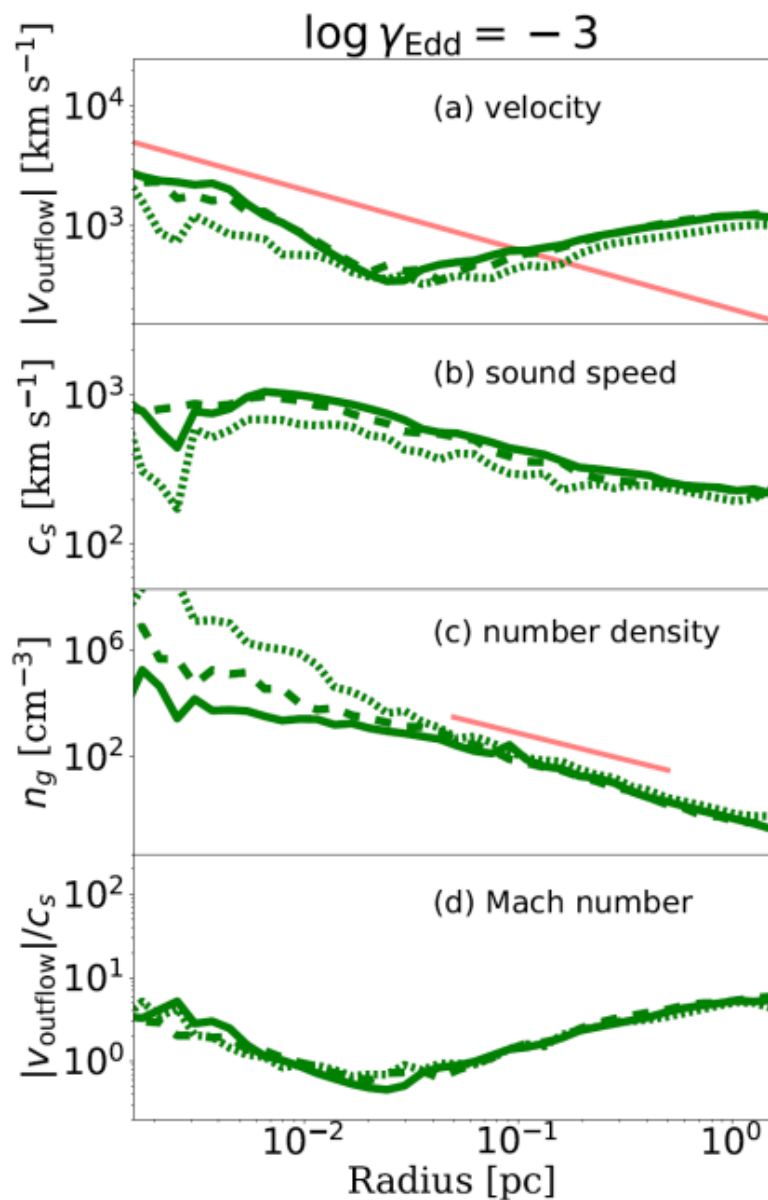
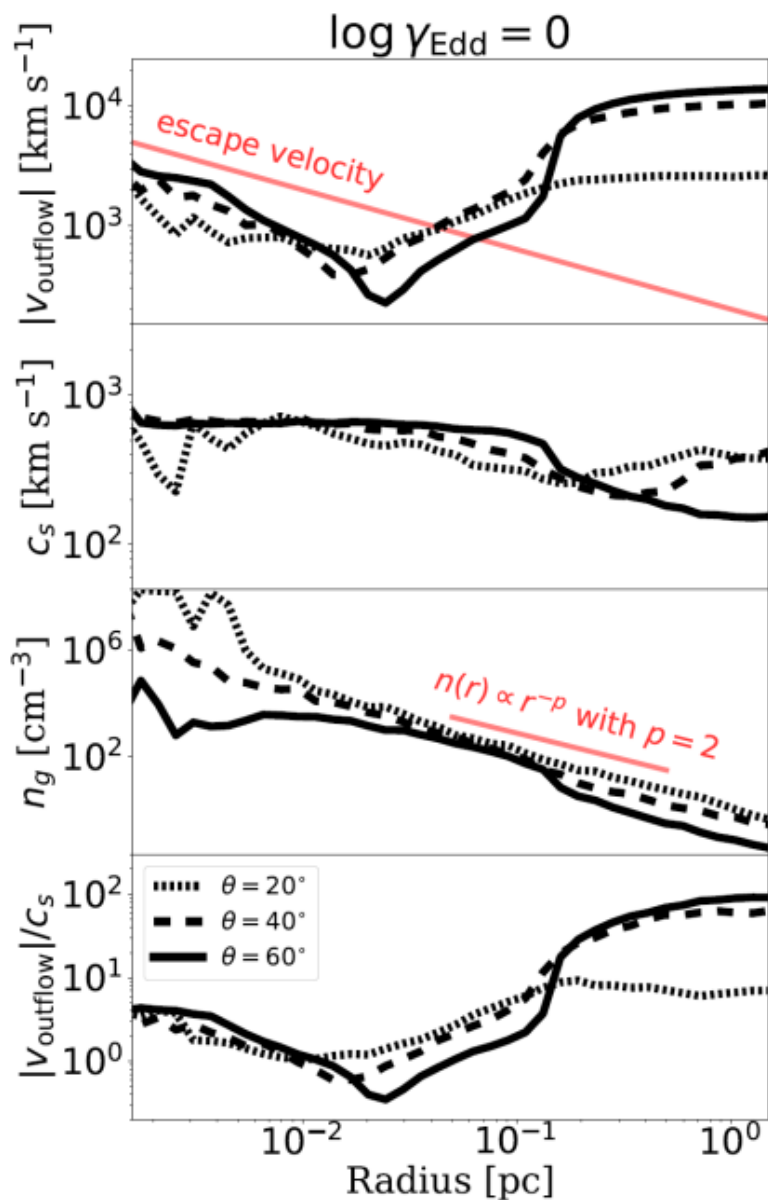
# Eddington ratio dependence



# Inclination angle dependence

Radiation driven wind

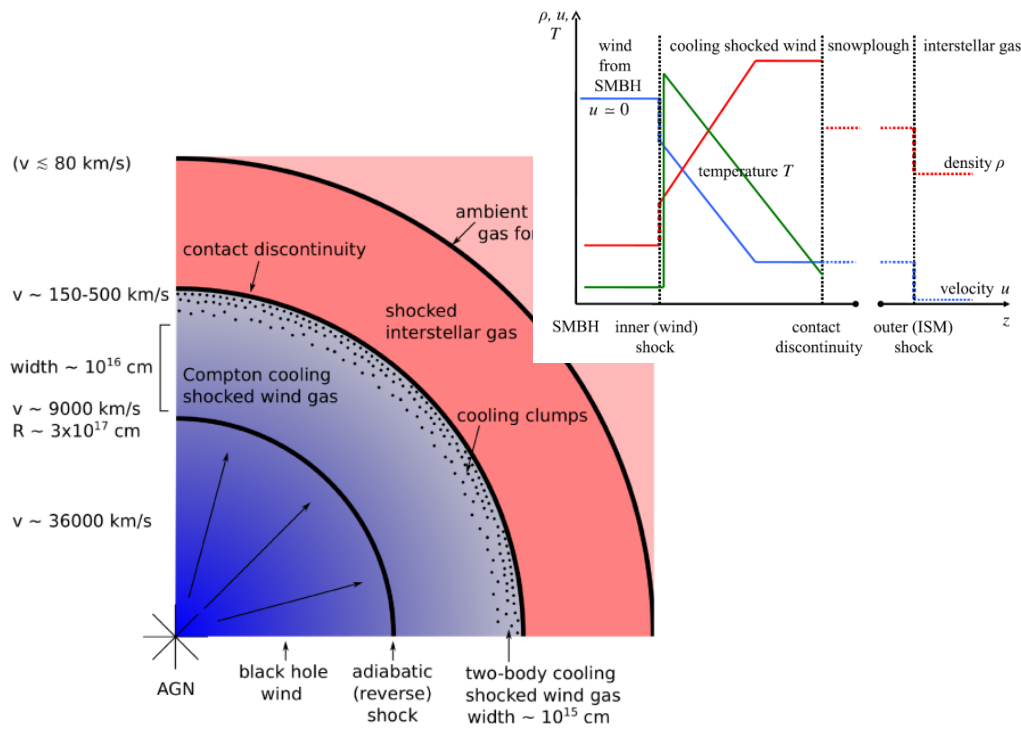
Thermal wind



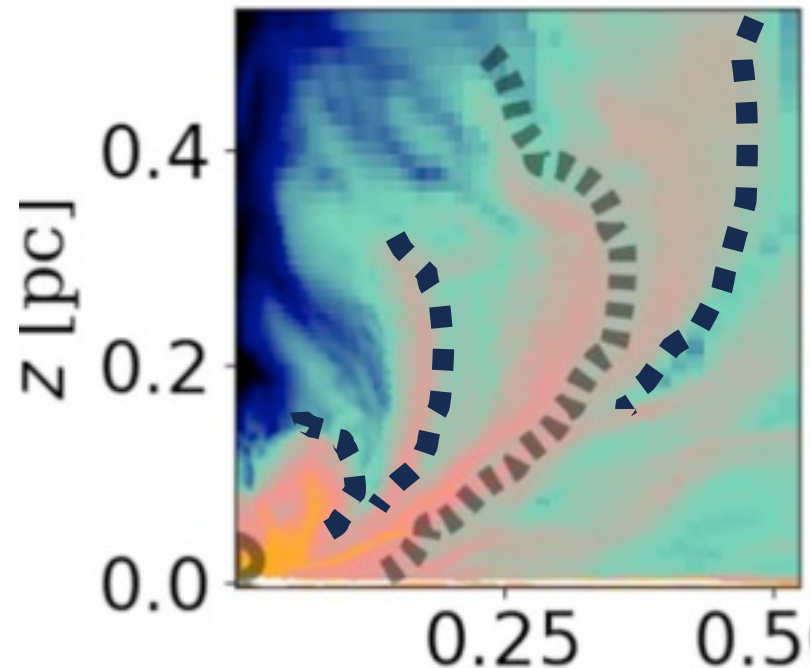
# Dynamic structure of ionized dusty outflow

We clarify an analytical model of ionized dusty outflow characterized by repetitive shell formation.

Shock propagation model  
King 2014, 2015



Ionized dusty outflow  
Kudoh et al. 2023



# What is happening around sub-pc (dust sublimation) scale?

Exceeding escape velocity due to dust radiation force

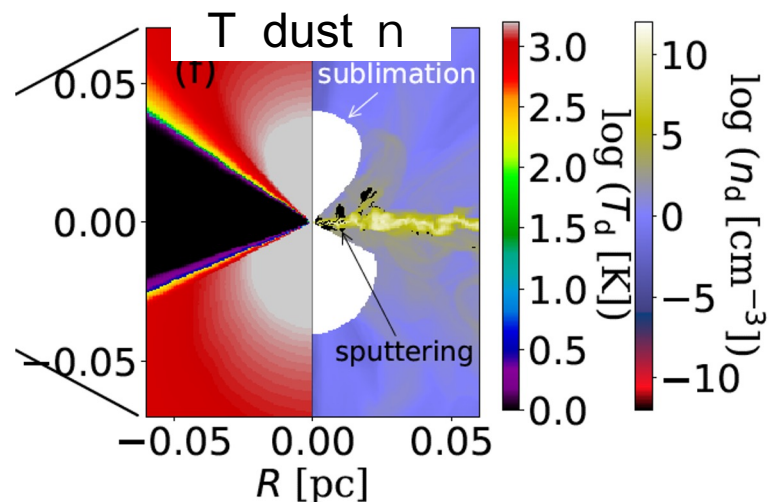
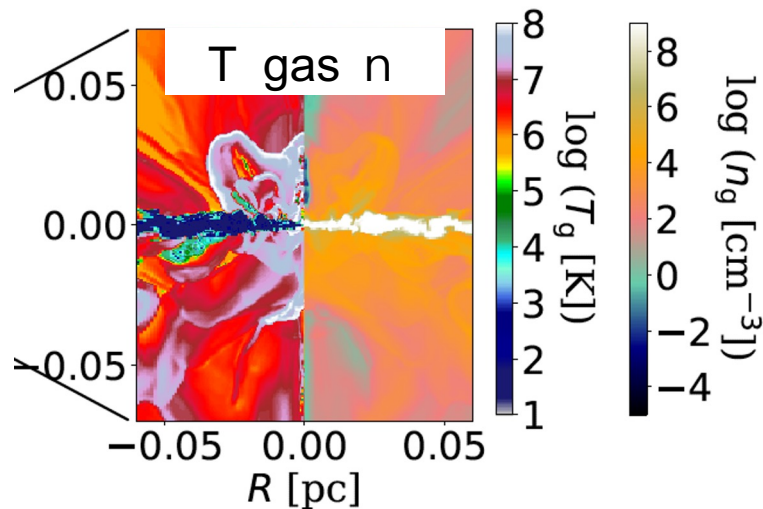
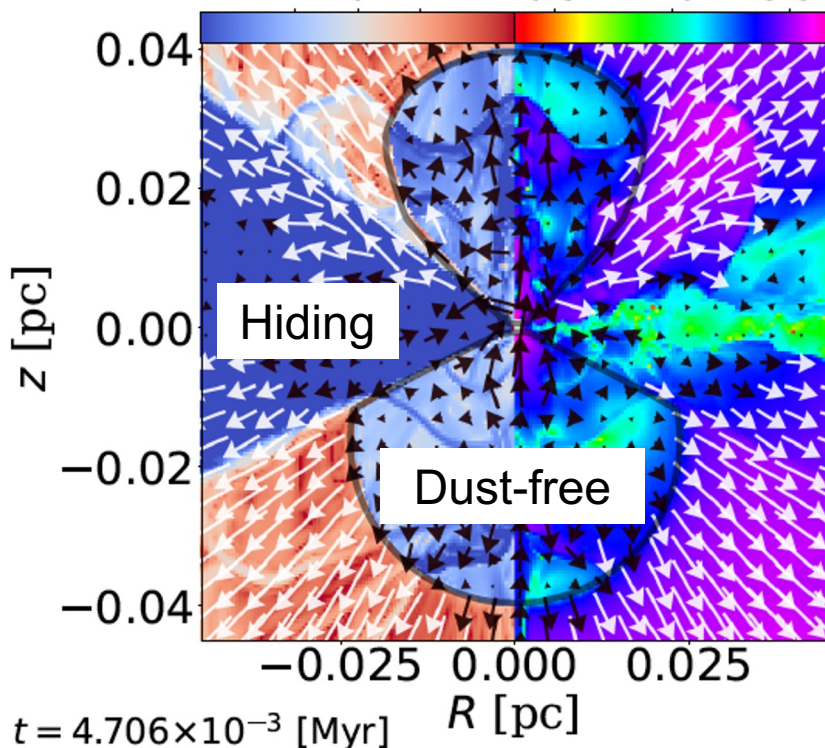
Red : Radiation force

Blue : Gas pressure force

Magnitude of

Poloidal velocity

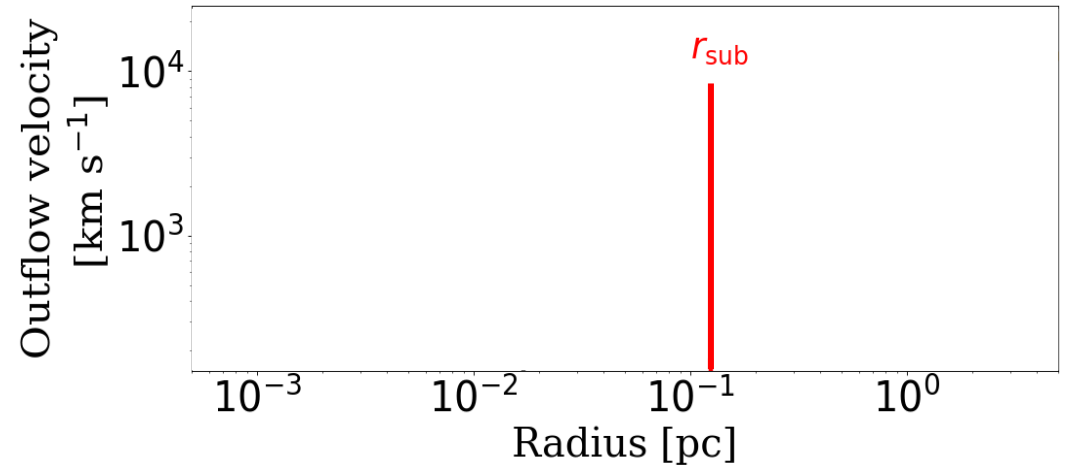
$\log(|\mathbf{f}_{\text{rad}}|/|\mathbf{f}_{\text{pg}}|)$        $\log(v_{\text{outflow}} [\text{km s}^{-1}])$   
 -1 0 1      0.5 2.0 3.5



# Procedure

AGNs with known

- $Y_{\text{Edd}}$ : Eddington ratio
- $M_{\text{SMBH}}$ : BH masses



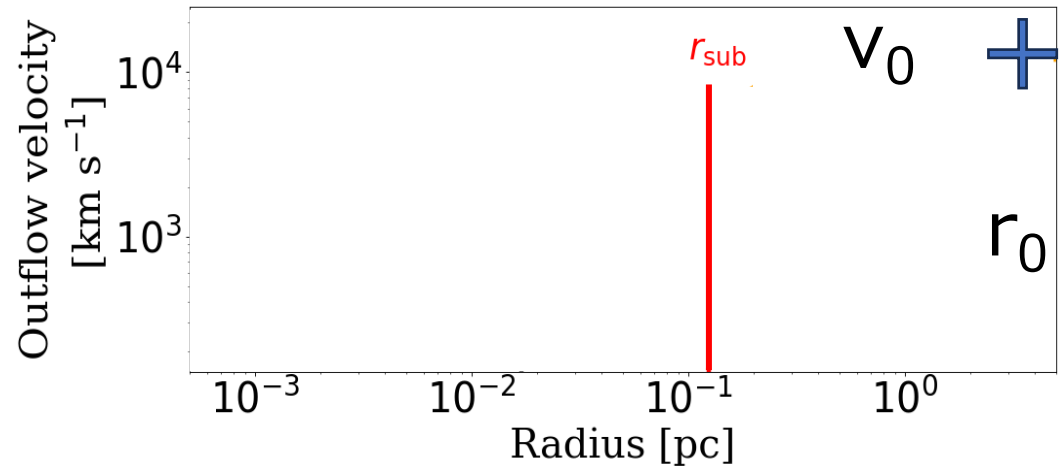
0. Estimate the dust sublimation radius.

$$r_{\text{sub}} = \sqrt{\frac{\delta_L L_{\text{bol}}}{4\pi\sigma_{\text{SB}}T_d^4}} \sim 0.176 \text{ pc} \left(\frac{\delta_L \gamma_{\text{Edd}}}{0.5}\right)^{1/2} \left(\frac{M_{\text{SMBH}}}{10^7 M_{\odot}}\right)^{1/2} \left(\frac{T_d}{1500 \text{ K}}\right)^{-2}$$

# Procedure

AGNs with known

- $\Upsilon_{\text{Edd}}$ : Eddington ratio
- $M_{\text{SMBH}}$ : BH masses



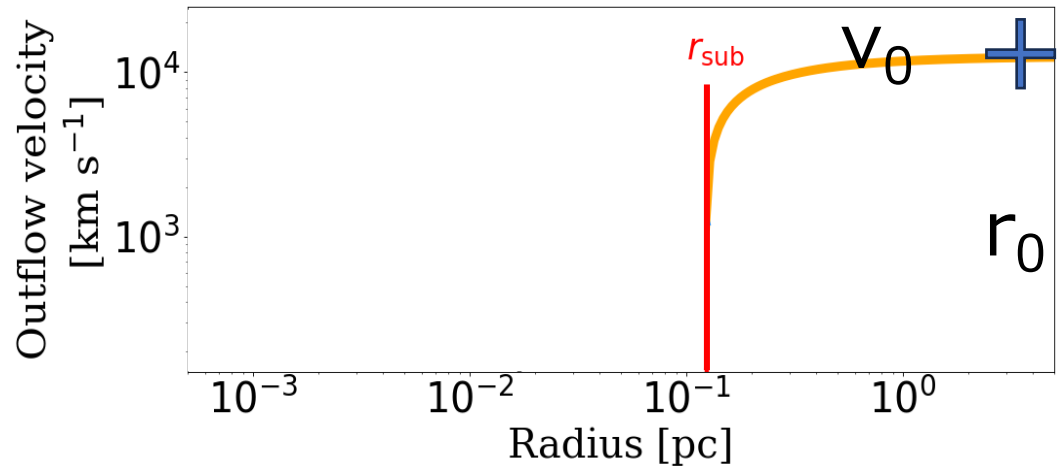
0. Estimate the dust sublimation radius.

1. The observed velocity is considered the terminal velocity,  $v_0$ .  
(Temperature information is also desirable.)

→ Given  $r_0$  and  $v_0$ .

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + (\Gamma_{\text{Edd}} - 1) \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)$$

# Procedure



AGNs with known

- $\Upsilon_{\text{Edd}}$ : Eddington ratio
- $M_{\text{SMBH}}$ : BH masses

0. Estimate the dust sublimation radius.

1. The observed velocity is considered the terminal velocity.  
(Temperature information is also desirable.)

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + (\Gamma_{\text{Edd}} - 1) \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)$$

2. For  $r > r_{\text{sub}}$ , apply the **Dusty wind** solution.

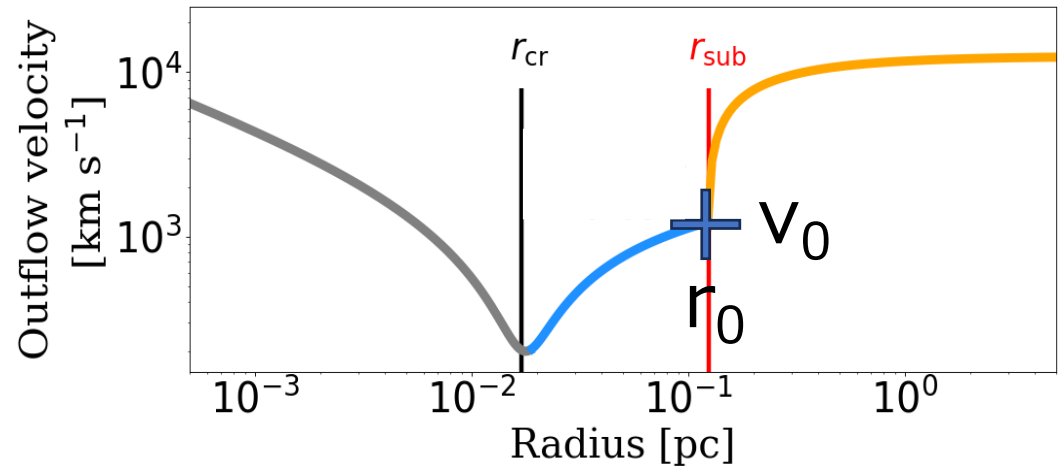
$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + \Gamma_{\text{Edd,d}} \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right]$$

$$\Gamma_{\text{Edd,d}} = \frac{\kappa}{\kappa_T} \delta_L \gamma_{\text{Edd}} = \frac{\text{Dust radiation force}}{\text{Gravity force}}$$

# Procedure

AGNs with known

- $\Upsilon_{\text{Edd}}$ : Eddington ratio
- $M_{\text{SMBH}}$ : BH masses



0. Estimate the dust sublimation radius.

1. The observed velocity is considered the terminal velocity. (Temperature information is also desirable.)

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + (\Gamma_{\text{Edd}} - 1) \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)$$

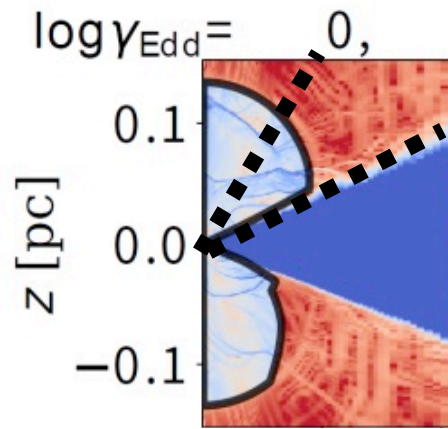
2. For  $r > r_{\text{sub}}$ , apply the **Dusty wind** solution.

3. For  $r < r_{\text{sub}}$ , apply the **Stellar wind** solution.

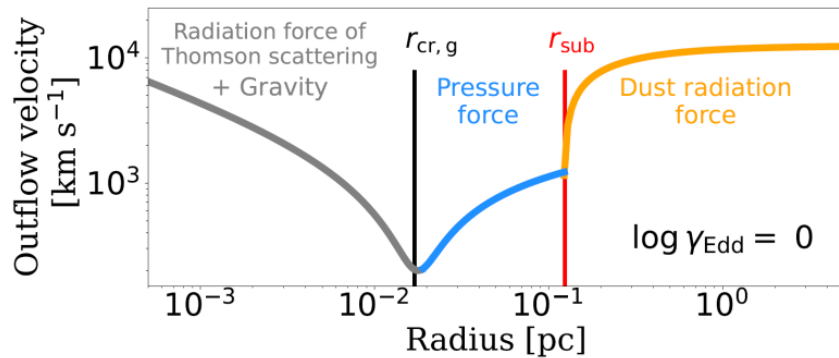
→ Given  $v_0$  and  $r_0$  at the dust sublimation radius

$$\left[ \frac{v(r)}{v_0} \right]^2 = 1 + (\Gamma_{\text{Edd,g}} - 1) \left( \frac{r_g}{r_0} \right) \left( \frac{c}{v_0} \right)^2 \left[ 1 - \left( \frac{r}{r_0} \right)^{-1} \right] + \frac{1}{\gamma} \left( \frac{c_s}{v_0} \right)^2 \ln \left( \frac{r}{r_0} \right)$$

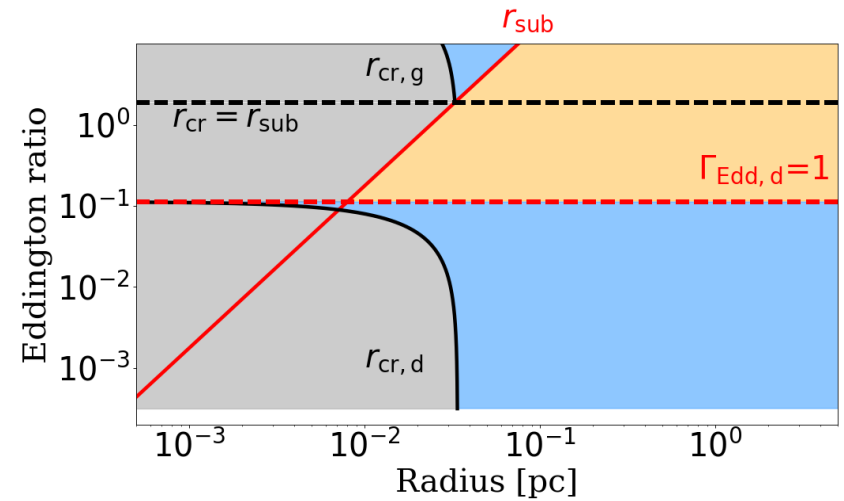
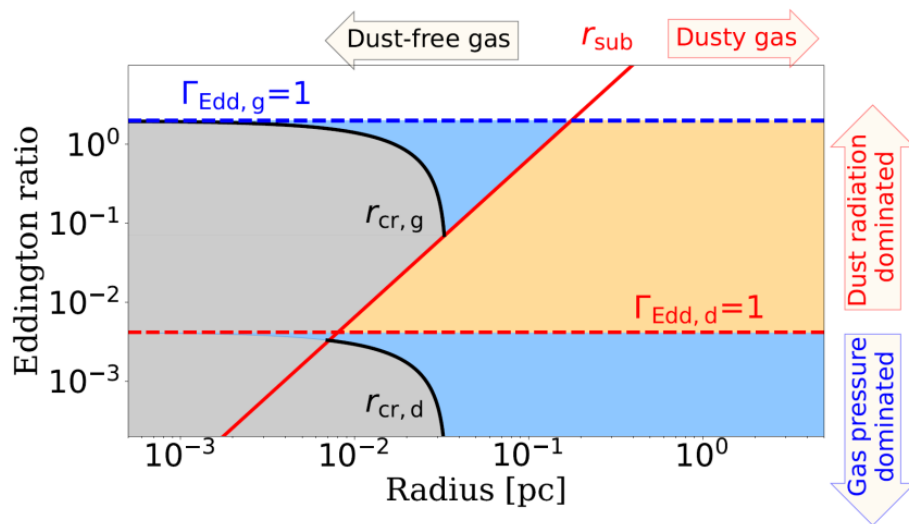
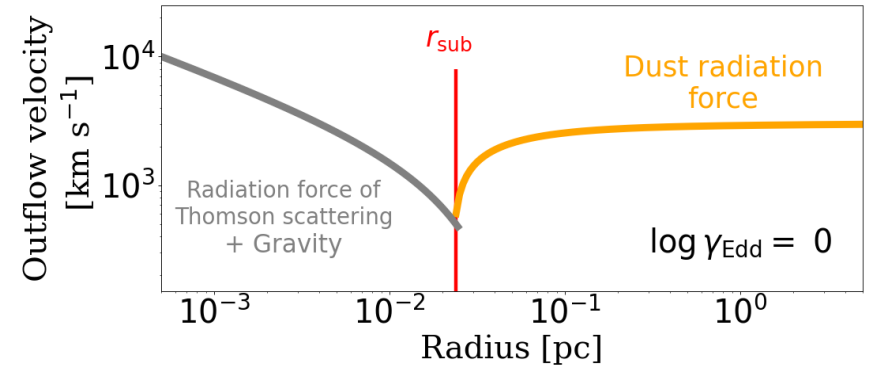
# Analytic solution



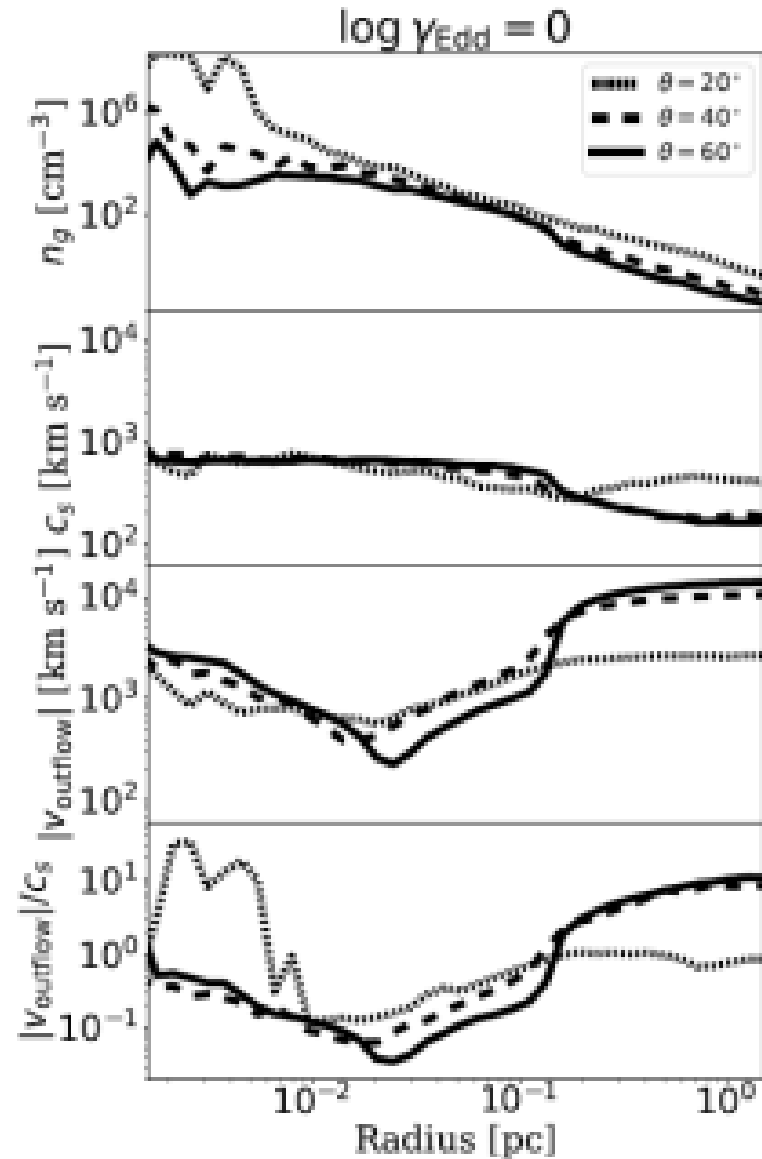
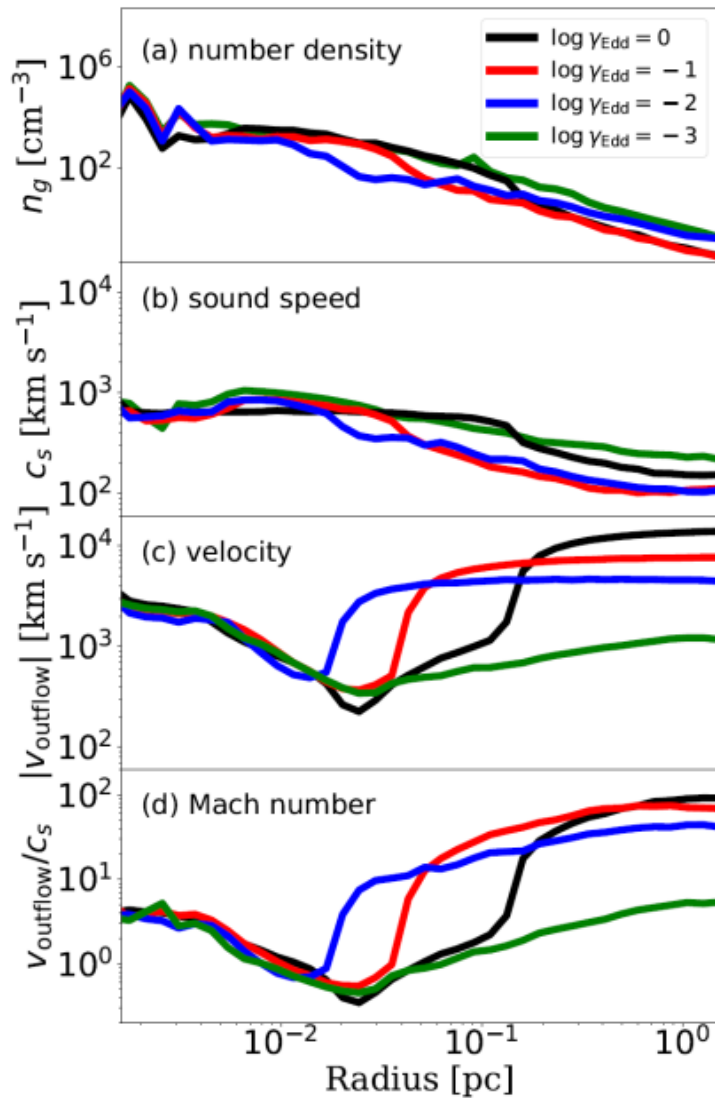
60 degree



30 degree



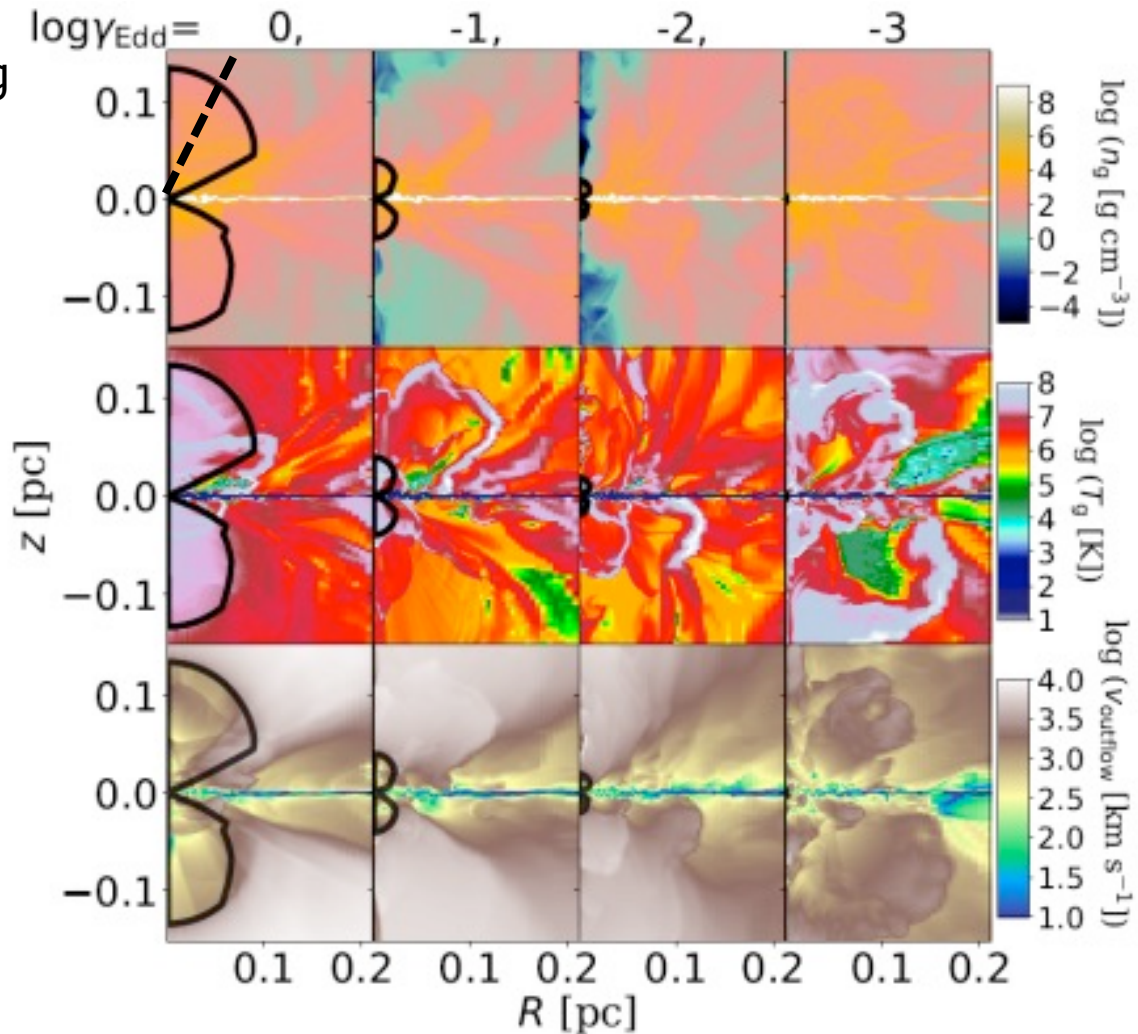
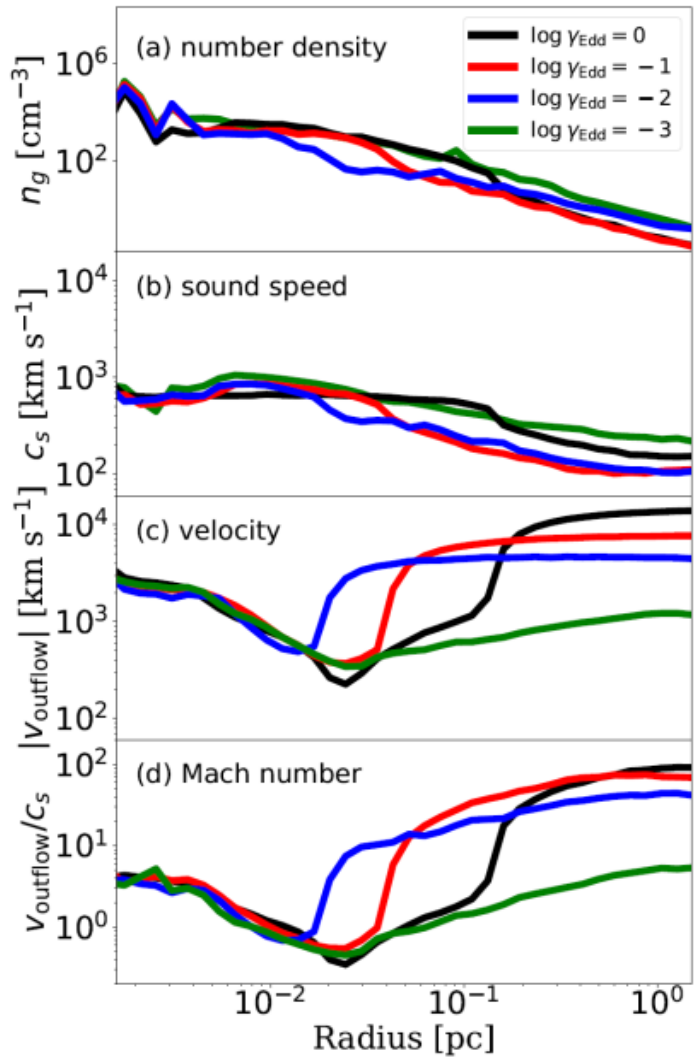
# Inclination angle



# Time averaged outflows are similar

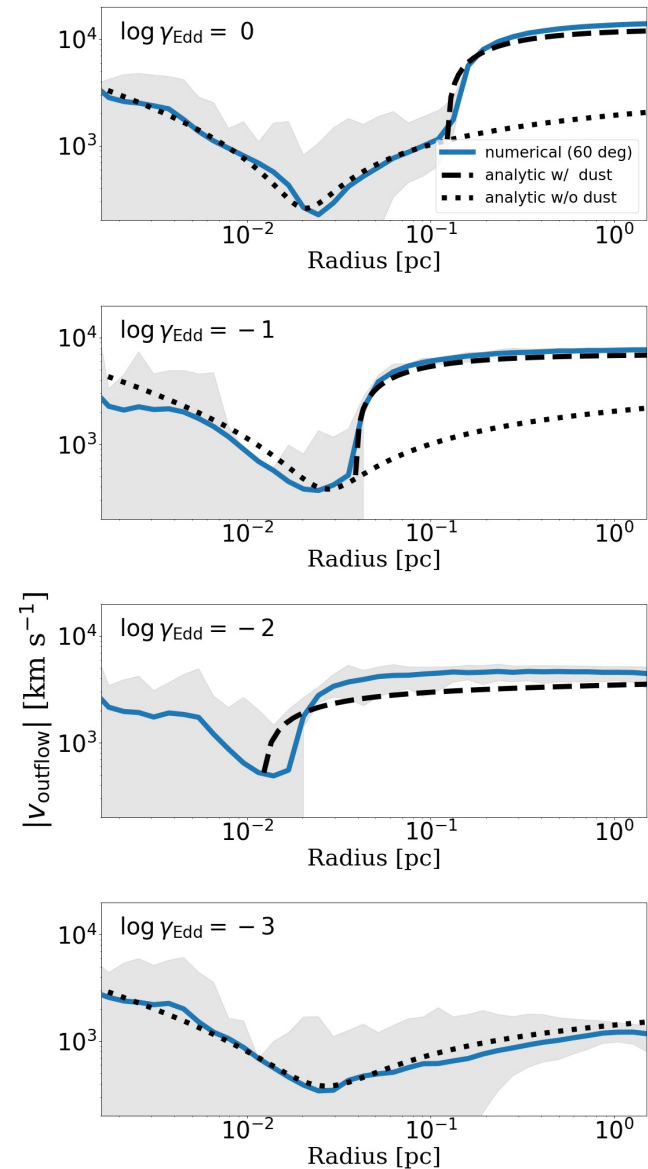
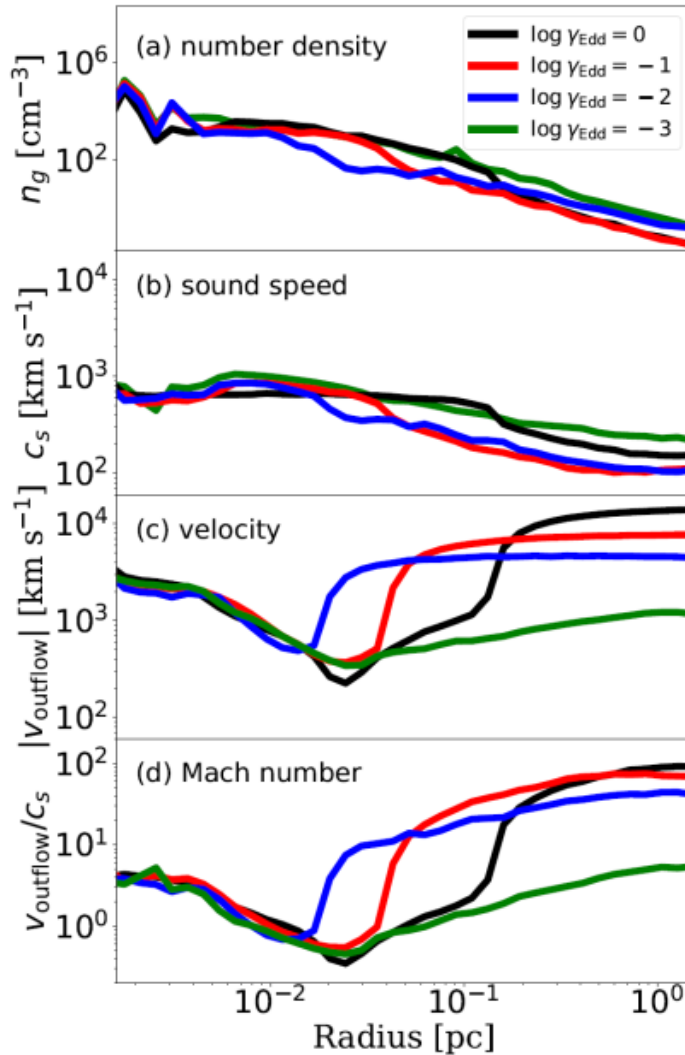
Snapshots in R-z plane

Time-averaged  
Radial profile at 60 deg



# Analytic solution vs Numerical solution

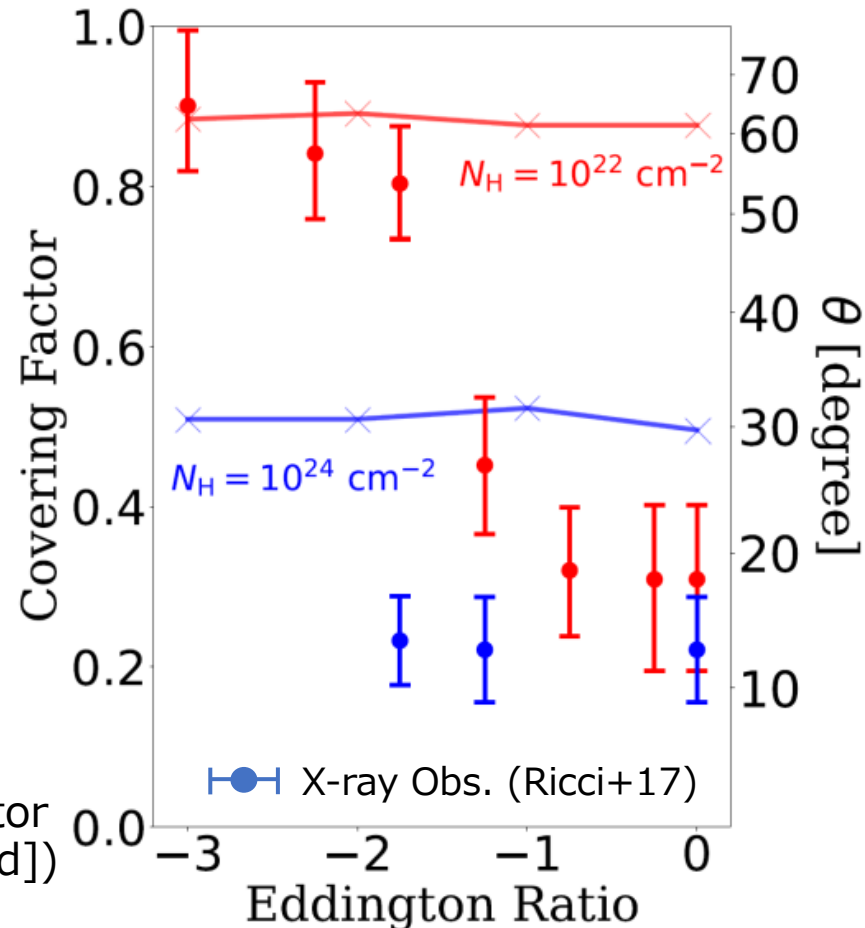
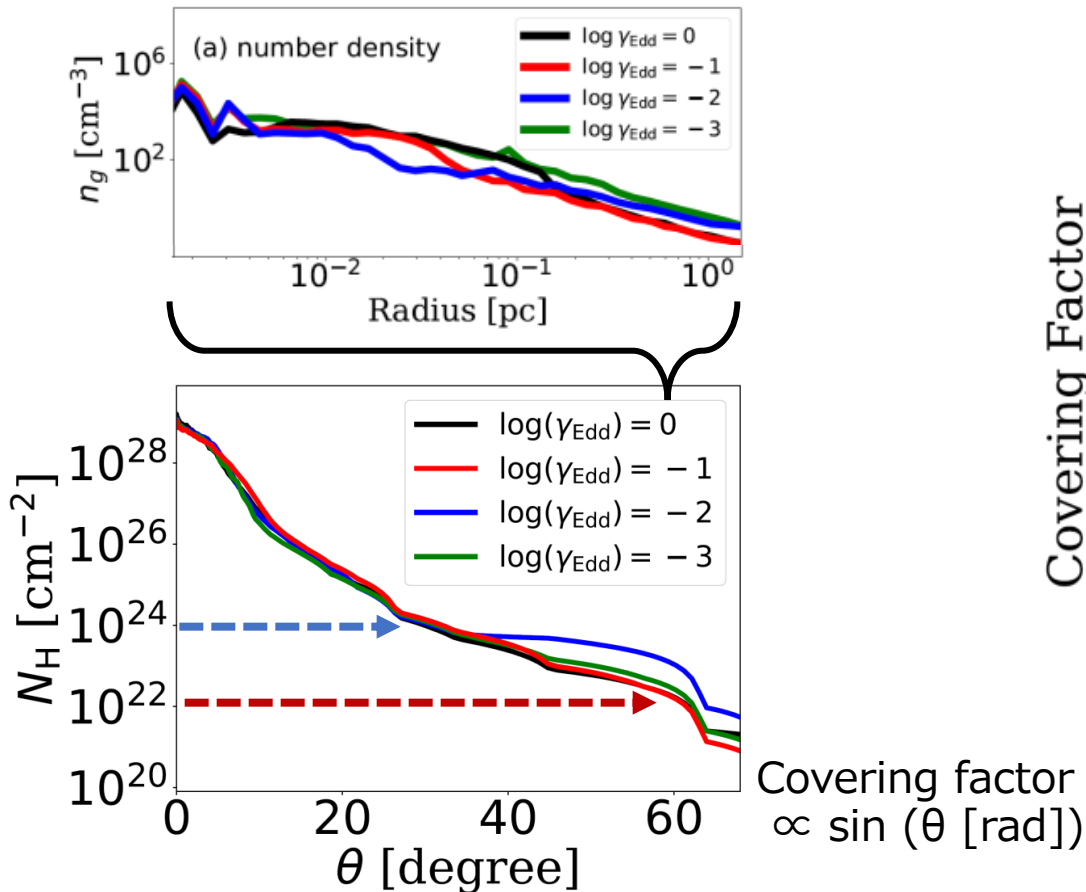
Time-averaged  
Radial profile at 60 deg



# Covering factor

## Column density: simulation vs observation

- Column density is determined by the sub-pc scale.
- The same r-profile  $\leftrightarrow$   $\theta$ -profile independent of the Eddington ratio.
- Large covering factor can be explained by our model.



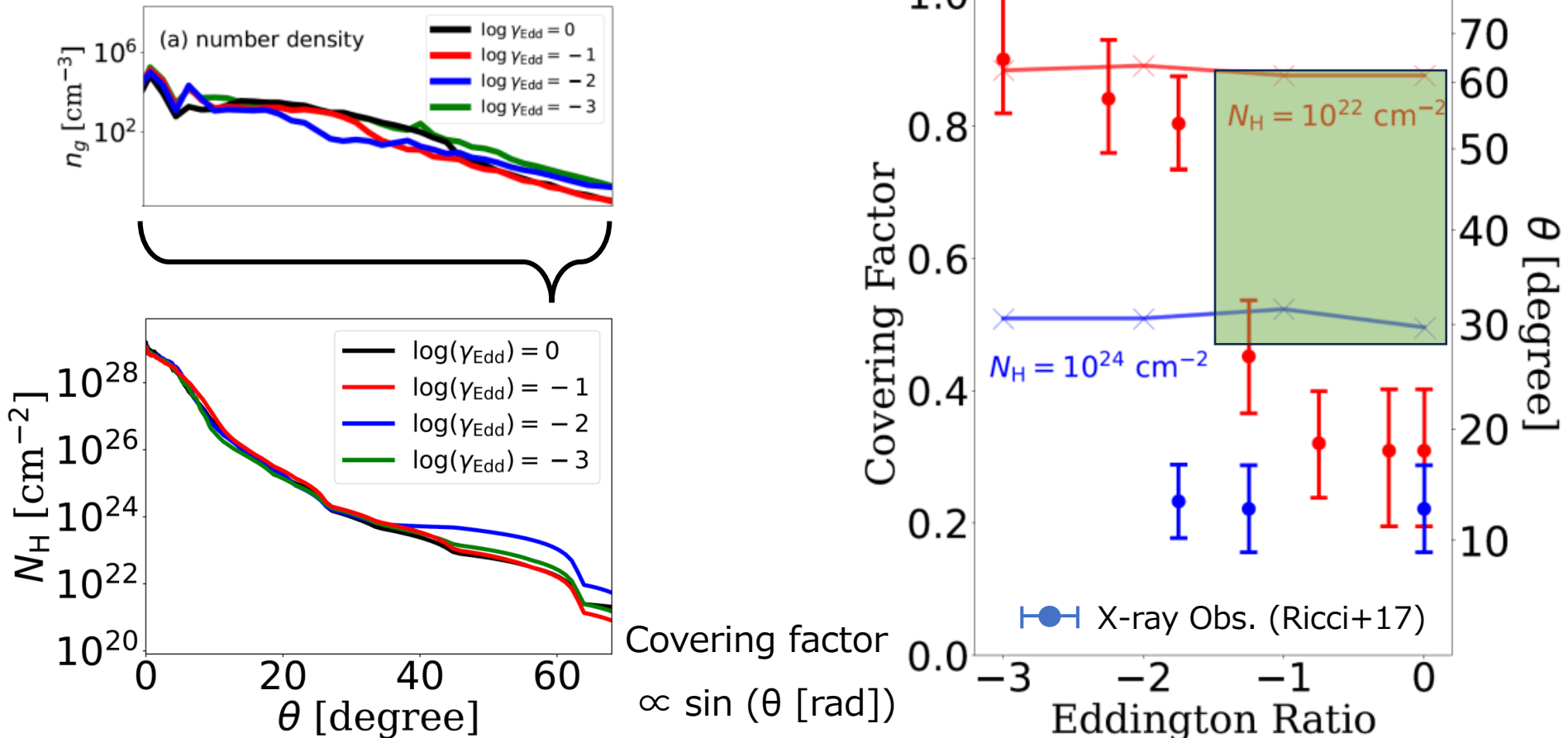
# Covering factor

## Column density: simulation vs observation

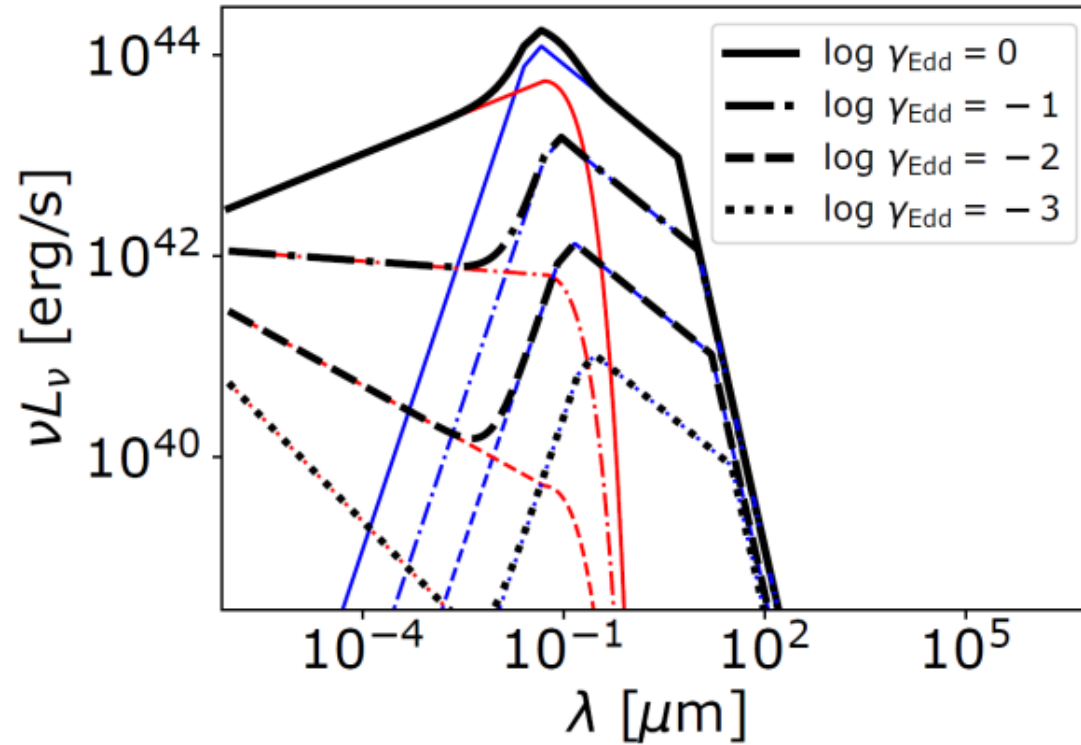
- Why is large Eddington ratio small CF?

→ Outflow from smaller than sub-pc scale.

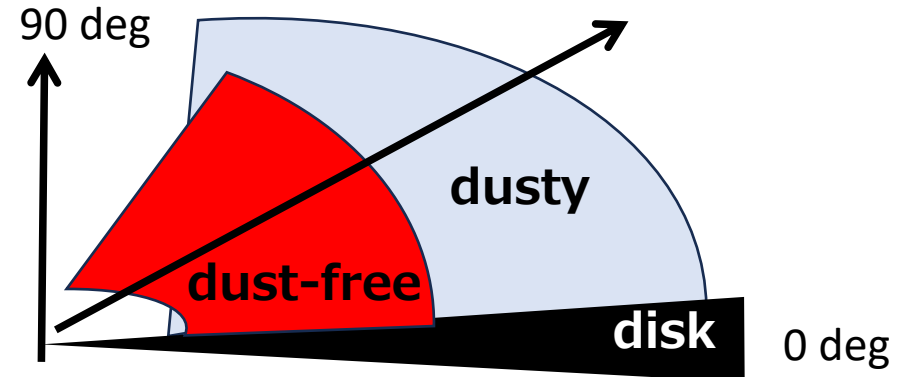
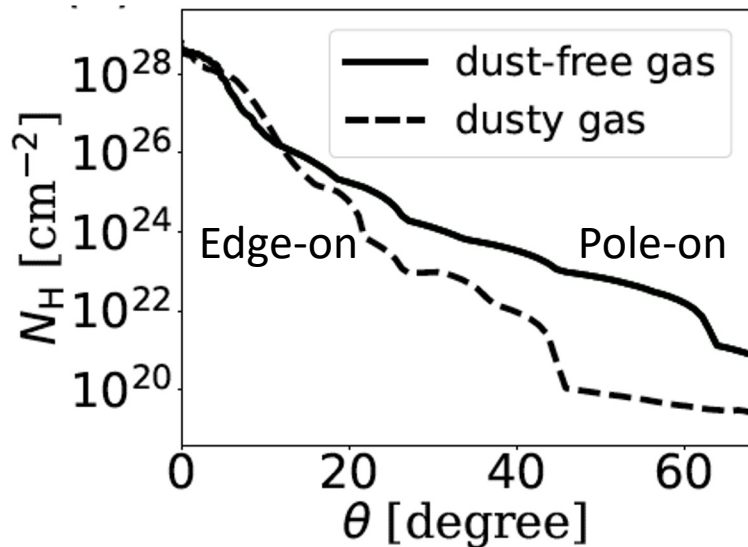
Line-driven outflow (e.g. Nomura+20) would blow out sub-pc-scale gas.



# Radiation field



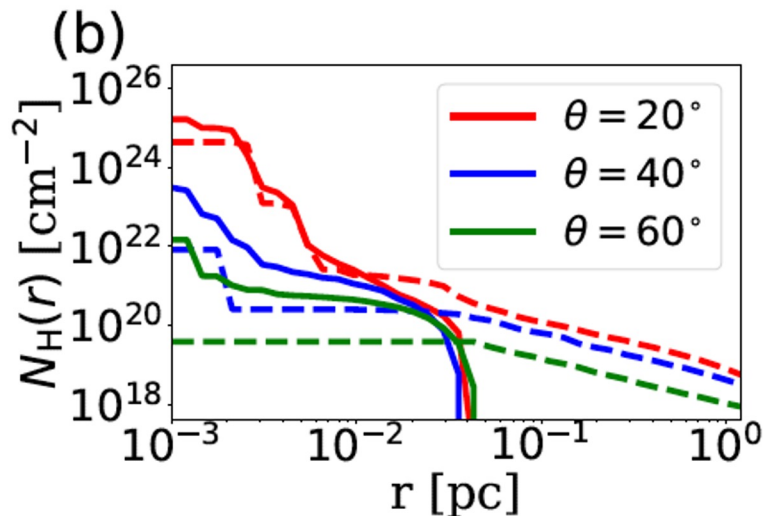
# Column density ( $L_{\text{bol}}/L_{\text{Edd}} = 10^{-1}$ ) for dust-free/dusty gases



- Column density is determined by **dust-free gas** inside the dust sublimation radius.

$$N_{\text{H}}(r) = \int_{2\text{pc}}^r n(l) dl$$

X線観測では dust-free gas をみてるだろう  
IRでは昇華半径外縁部の dusty outflow



# AGN outflows not pictured in AGN unified model

Sub-mm - IR

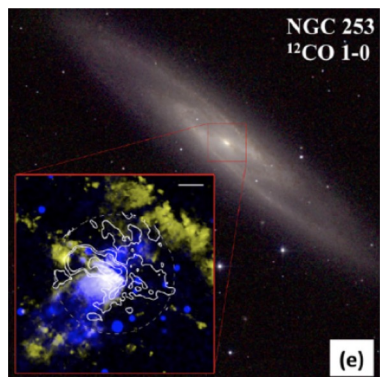
Opt - UV

X-ray

• Atomic/Molecular gas

Molecular outflow (10-100 km/s)

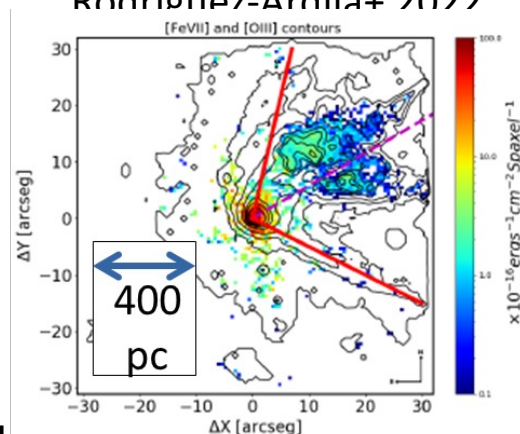
Bolatto+ 2013a, Veilleux+ 2020



• Ionized gas

(100-1000 km/s)

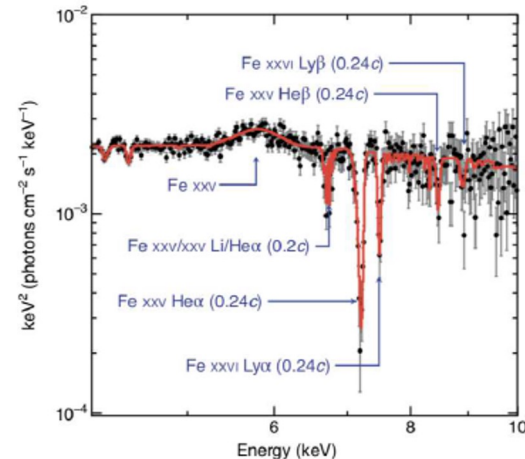
Rodríguez-Ardila+ 2022



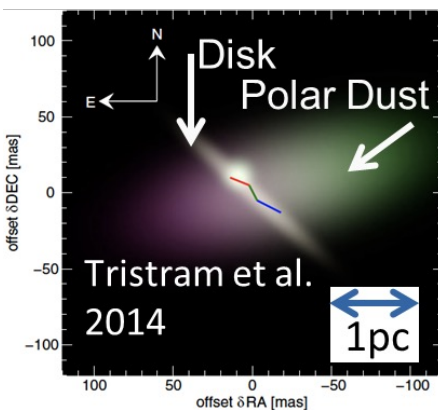
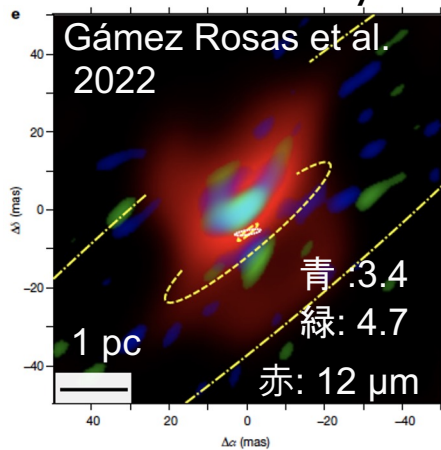
• High ionized metal

Ultra fast outflow (0.1c)

Ishia et al 2020

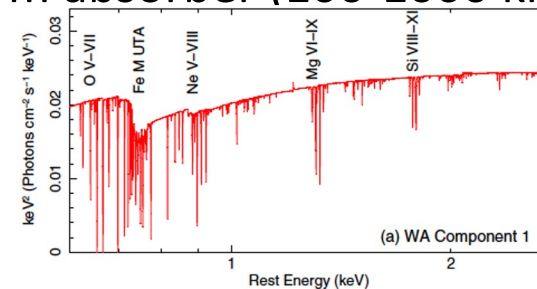


• Dusty outflow



• Low ionized metal

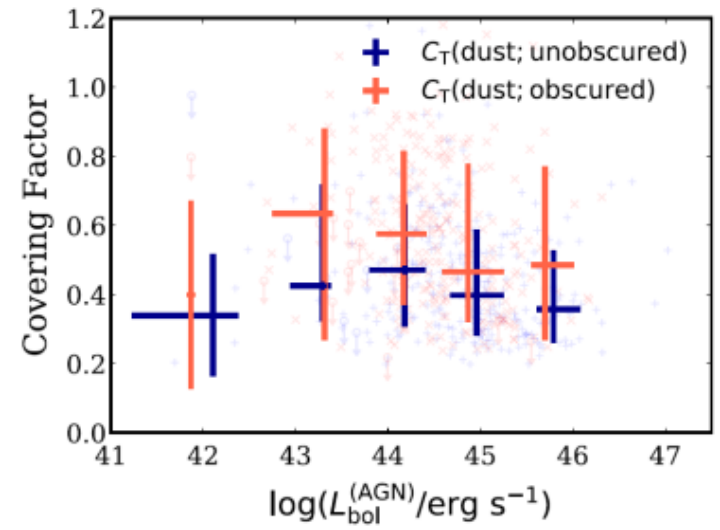
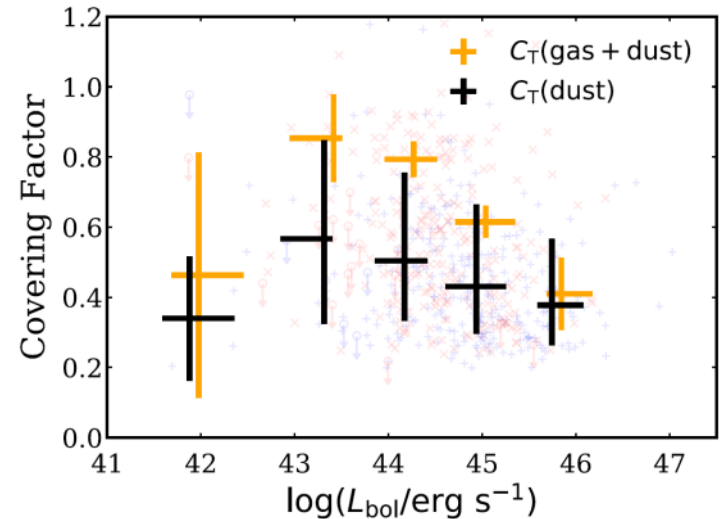
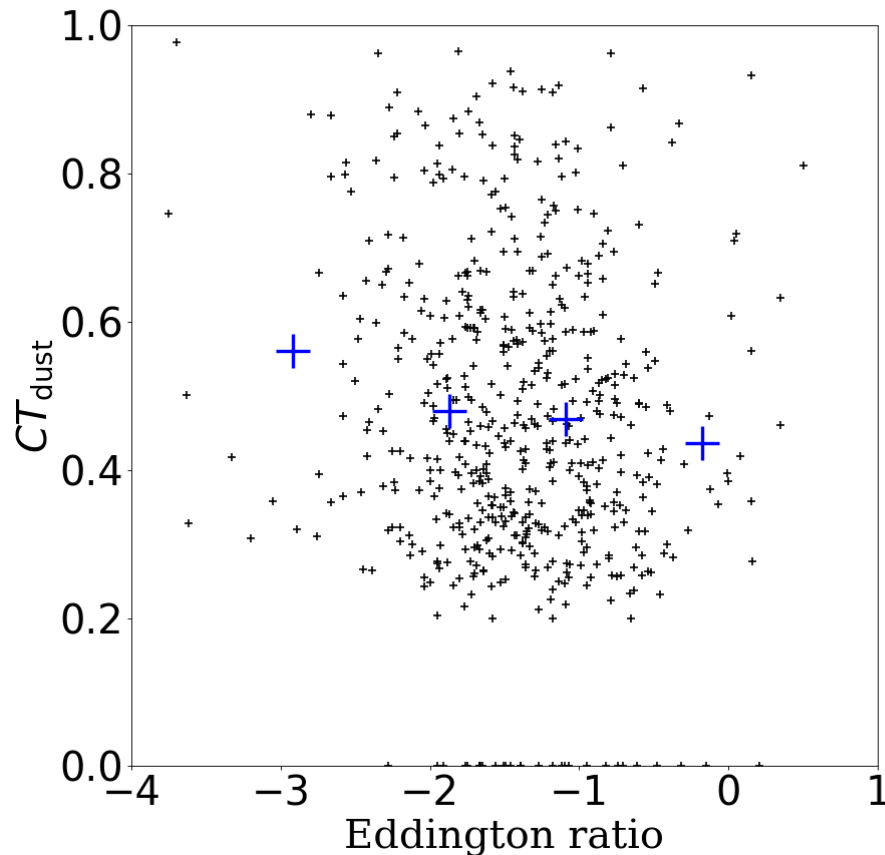
Warm absorber (100-1000 km/s)



# CF の Eddington ratio 依存性

Ichikawa+19 のダストCF  
Koss+22 の Eddington ratio

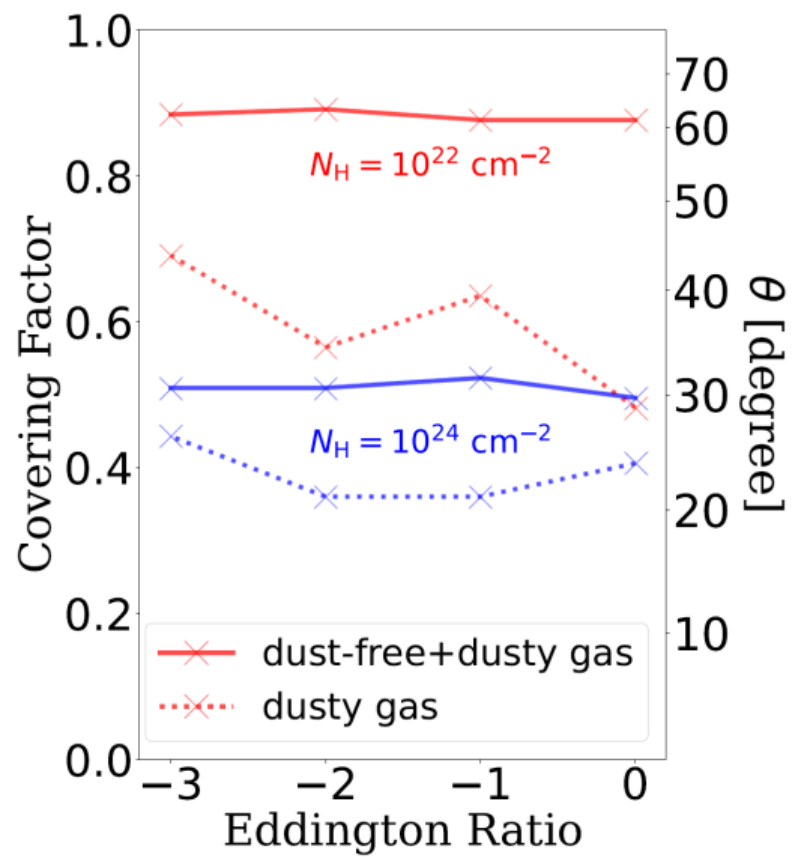
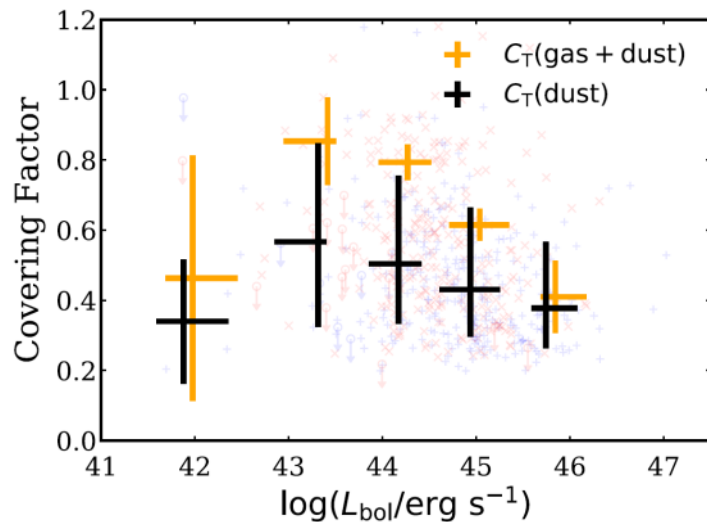
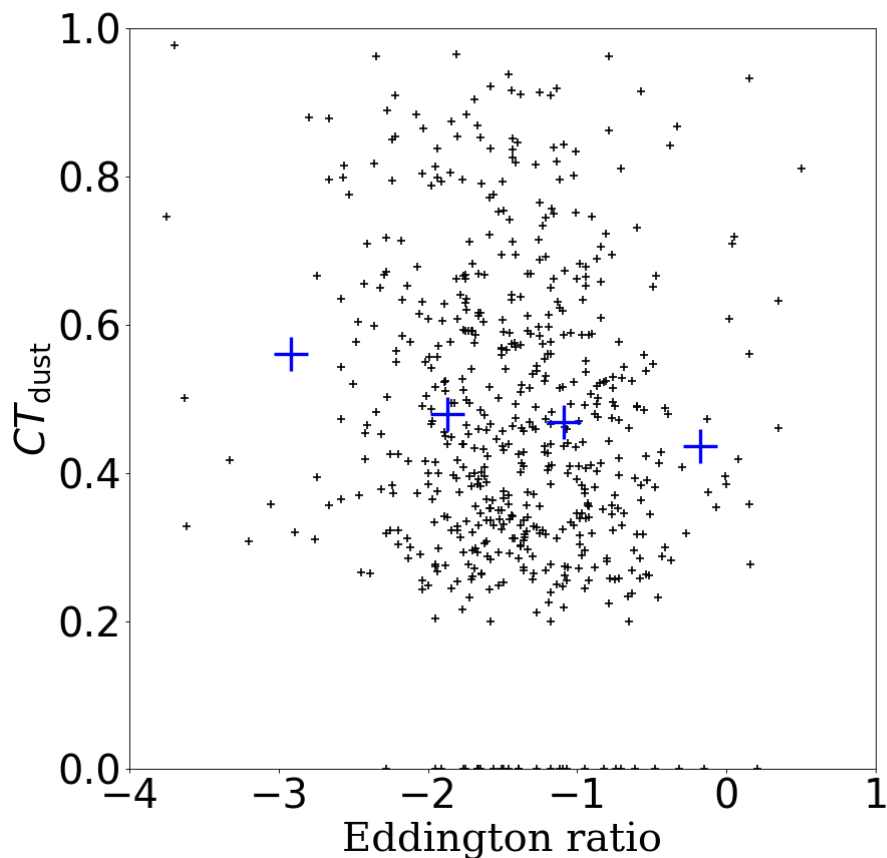
を組み合わせしてみた (天体の選択はIchikawa+19)



# CF の Eddington ratio 依存

Ichikawa+19 のダストCF  
Koss+22 の Eddington ratio

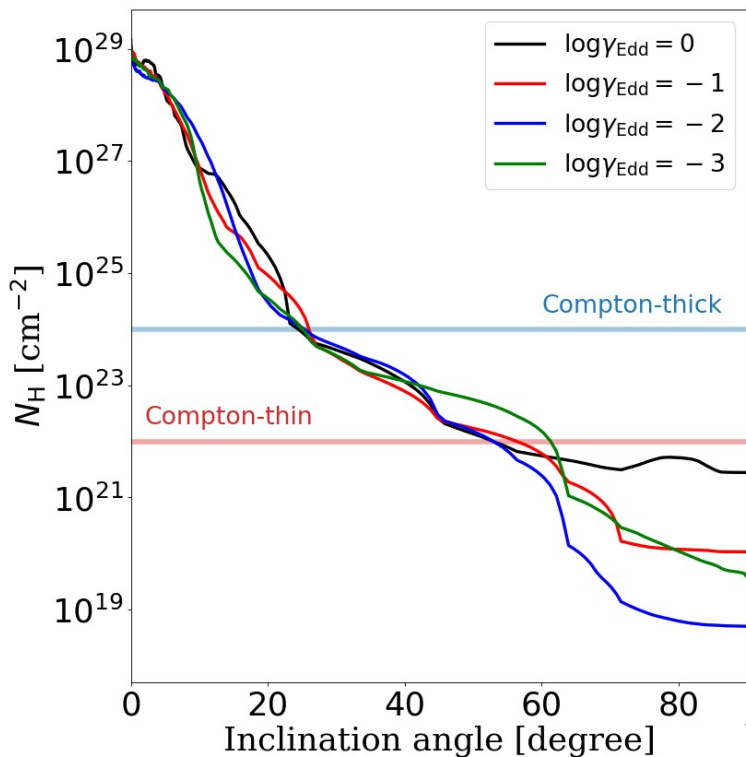
を組み合わせる



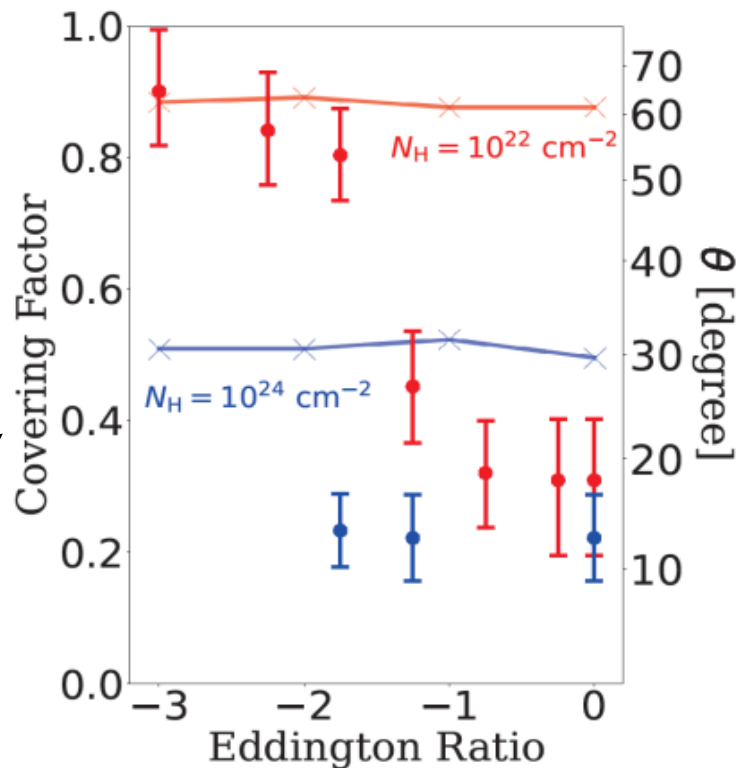
# Column density v.s. inclination angle

Column density  $N_H(\theta)$  as a function of angle  $\theta$  is

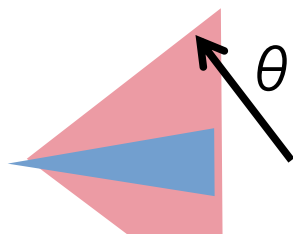
independent of Eddington ratio.



Convert to  
Covering factor  
 $CF = \sin \theta$



90 degree



0 degree

# Column density v.s. inclination angle

- X-ray observed CF is determined by dust-free gas.
- CF estimated by IR and X-ray would be different.

Decompose into dust-free gas (solid) and dusty gas (dotted)

